

(p,2p) Reactions on ^{9-16}C at 250 MeV/A

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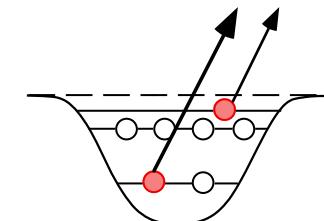
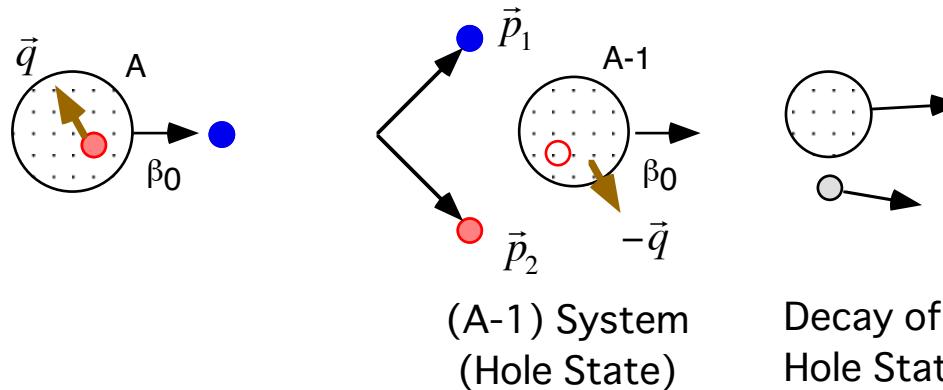
E. Takada

Single-Particle Motion in Unstable Nuclei

e beam: $(e, e' p)$

p beam: $(p, 2p)$, (p, pn)

Nucleon knockout Reactions, $(p, 2p)$ & (p, pn) , in Inverse Kinematics



Coincidence Measurements of forward particles

Decay Mode of Hole State with high efficiency

Nucleon knockout via quasi-free N-N scattering

Beam energy : need to be "high"

Measured Quantities

Momentum Distribution (\mathbf{q})

$$\vec{q}_{\perp} = (\vec{p}_1 + \vec{p}_2)_{\perp}$$

Angular Momentum (\mathbf{L})

$$\vec{q}_{\parallel} = \frac{(\vec{p}_1 + \vec{p}_2)_{\parallel} - \gamma \beta (M_A - M_{A-1})}{\gamma}$$

Separation Energy (E_s , $\mathbf{S_p}$)

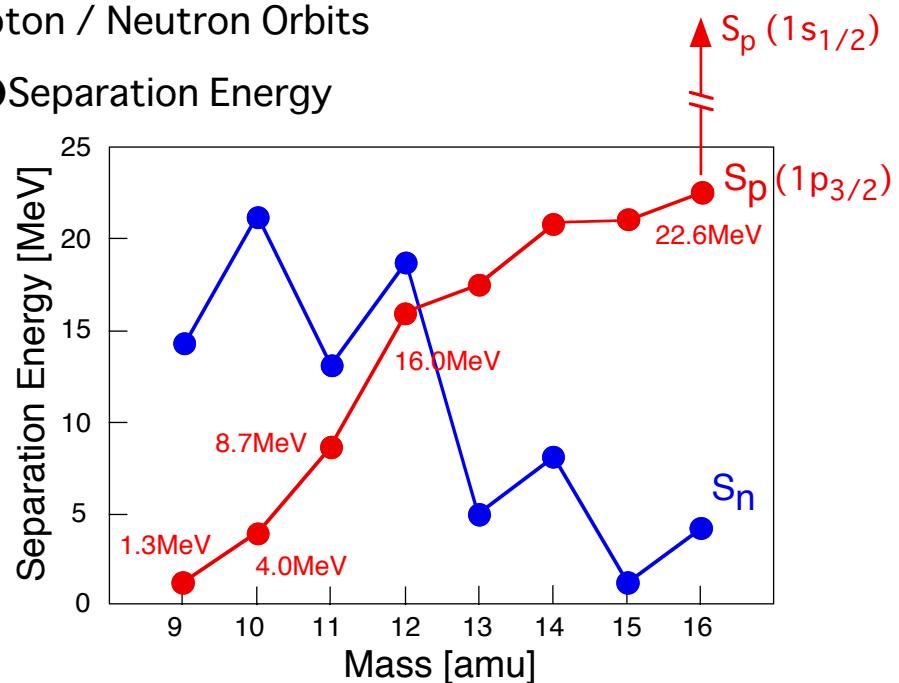
$$E_s = T_0 - \gamma (T_1 + T_2) - 2(\gamma - 1)m_p + \beta \gamma (\vec{p}_1 + \vec{p}_2)_{\parallel} - \frac{q^2}{2M_{A-1}}$$

Decay Mode of Hole States

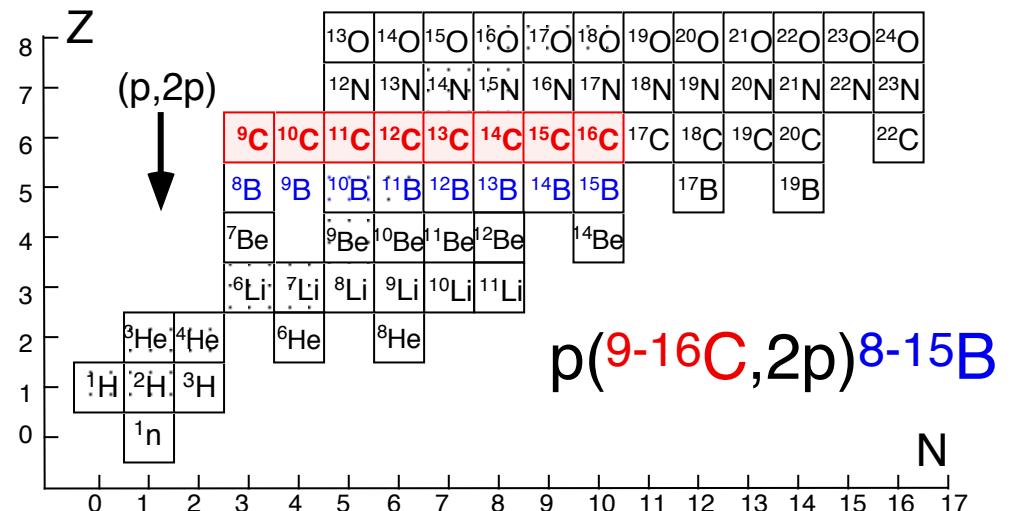
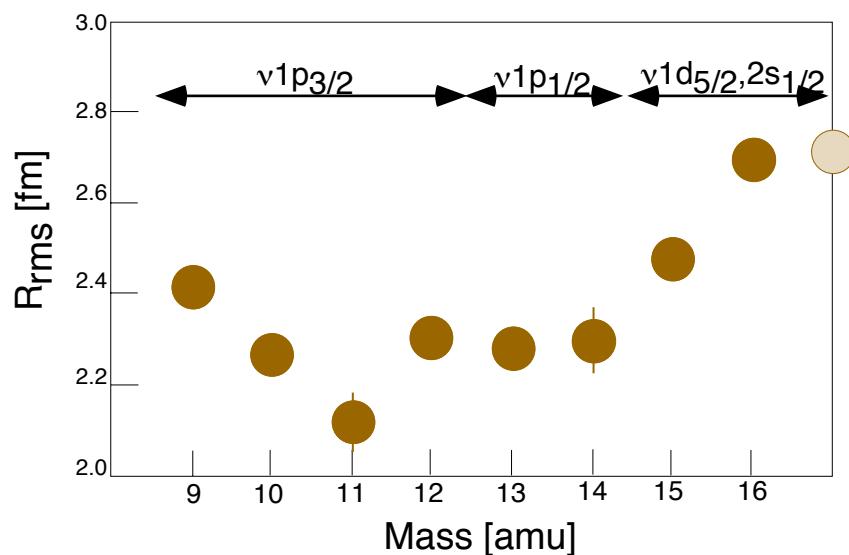
"Target" : Carbon Isotopes $^{9,10,11,12,13,14,15,16}\text{C}$

Proton / Neutron Orbits

● Separation Energy



● Root Mean Square (rms) Radii



○ Proton "p"-orbit ($L=1$) valence shell

Separation Energy :

Weakly-bound: $S_p(^9\text{C}) = 1.3 \text{ MeV}$
to
Strongly-bound: $S_p(^{16}\text{C}) = 22.6 \text{ MeV}$

○ Proton "s"-orbit ($L=0$) inner-shell

deeply-bound ($S_p = 30-50 \text{ MeV}$)

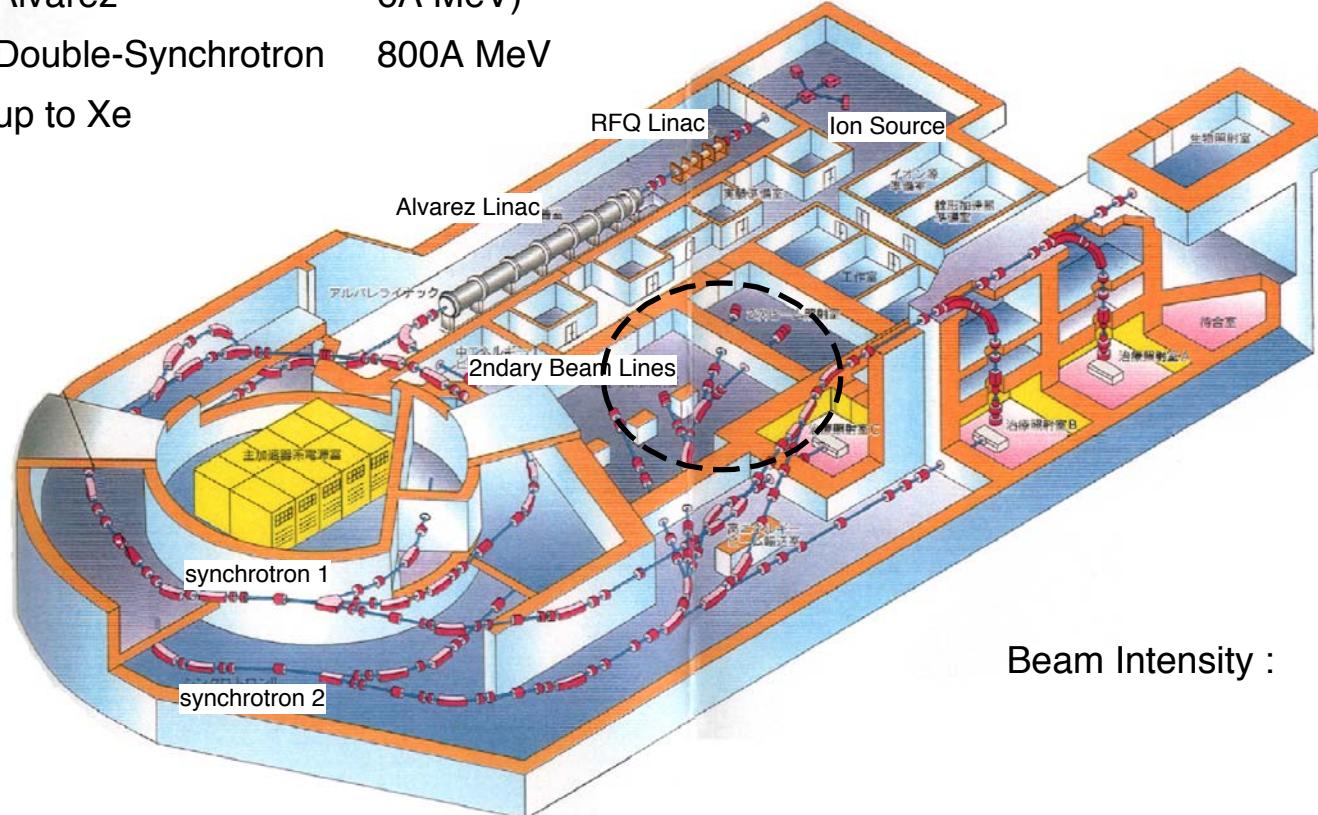
Accelerator Facility for Cancer Therapy

RFQ 0.8A MeV

Alvarez 6A MeV

Double-Synchrotron 800A MeV

up to Xe

Beam Intensity : C : $1.8 \times 10^9 / \text{sec}$ O : $1.1 \times 10^9 / \text{sec}$

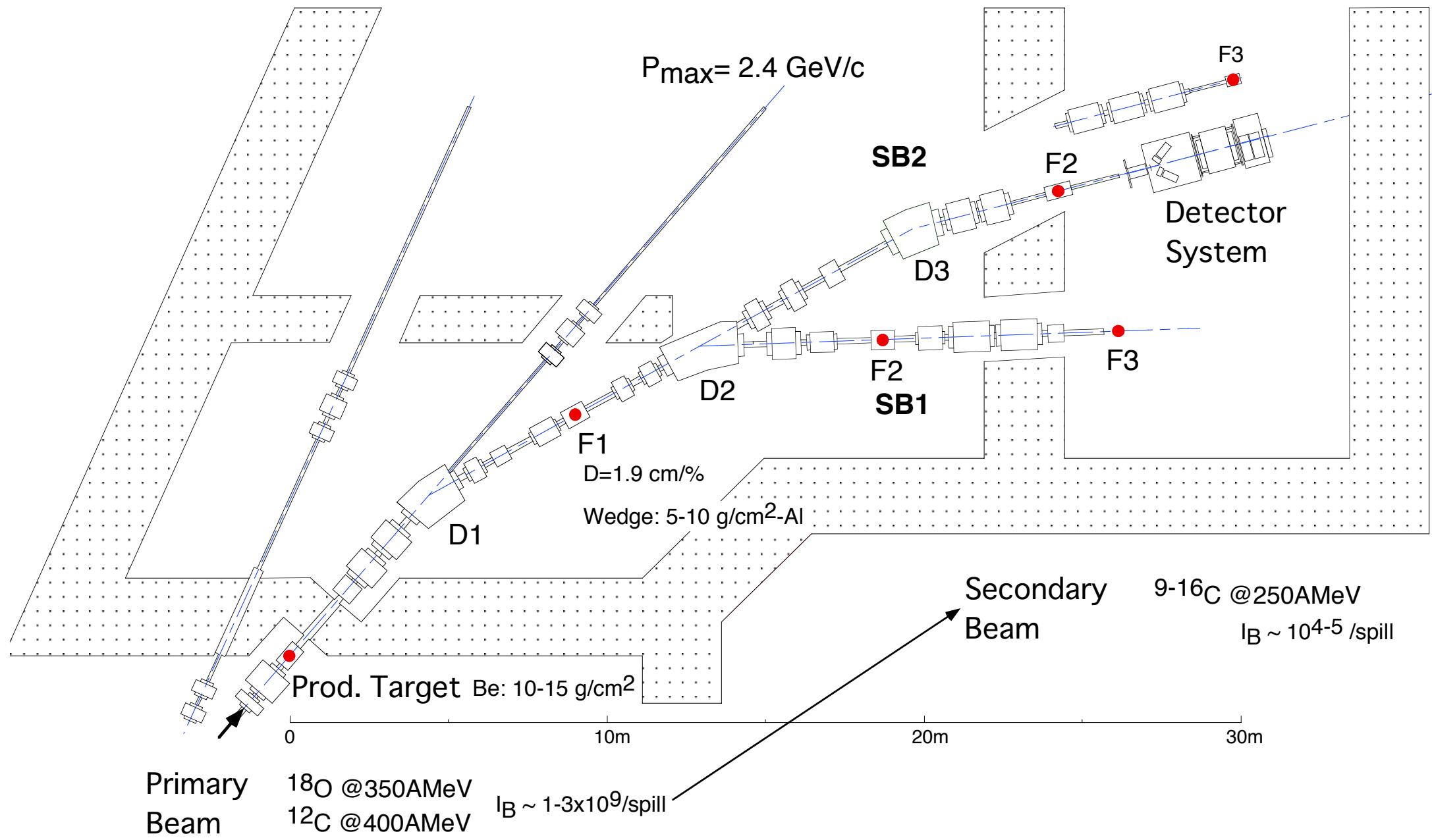
Beam Structure

Repetition Rate : $(3.3 \text{ sec})^{-1}$

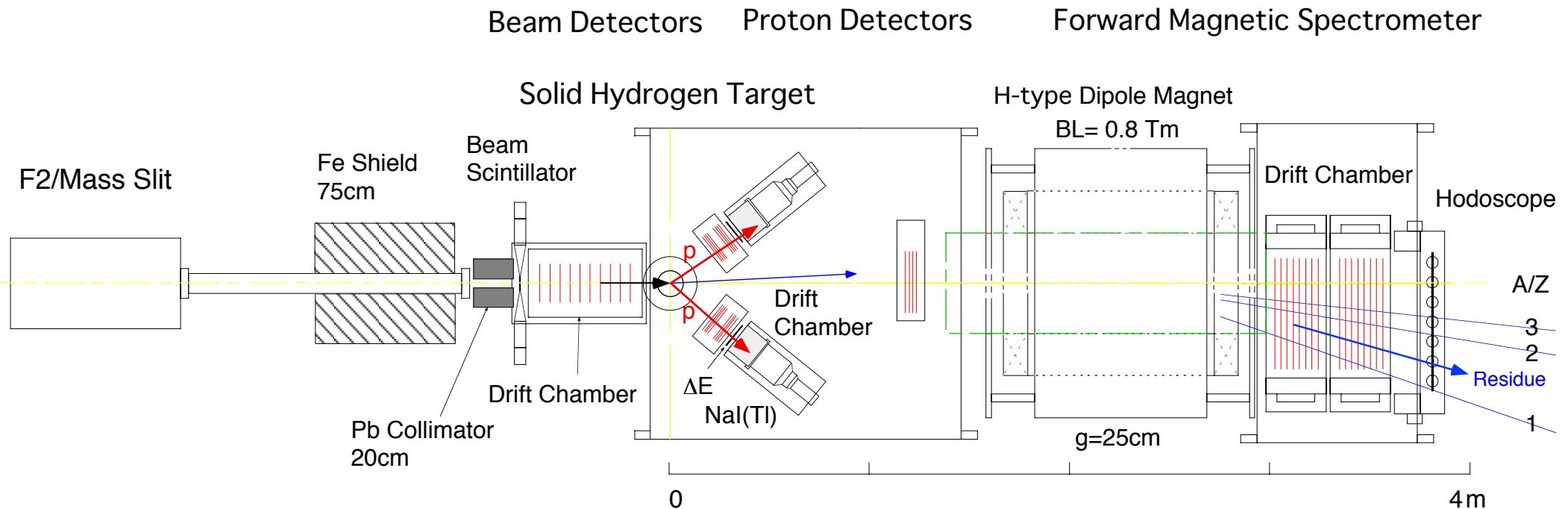
Duty factor : 30-50 %

Slow Extraction : debunched beam:

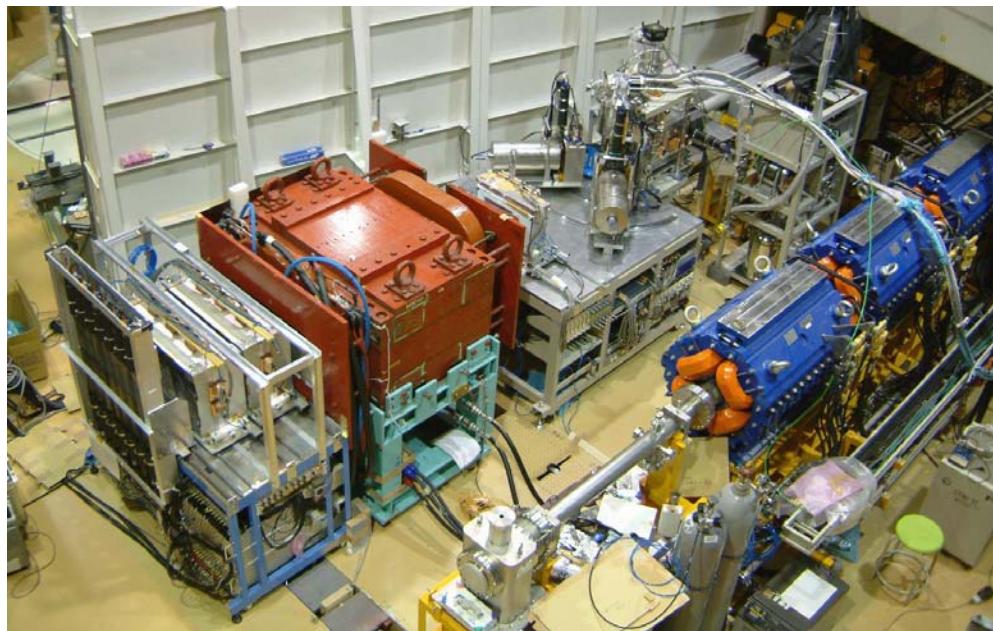
Secondary Beam Lines @HIMAC



Experimental Setup @F3



Setup seen from downstream side

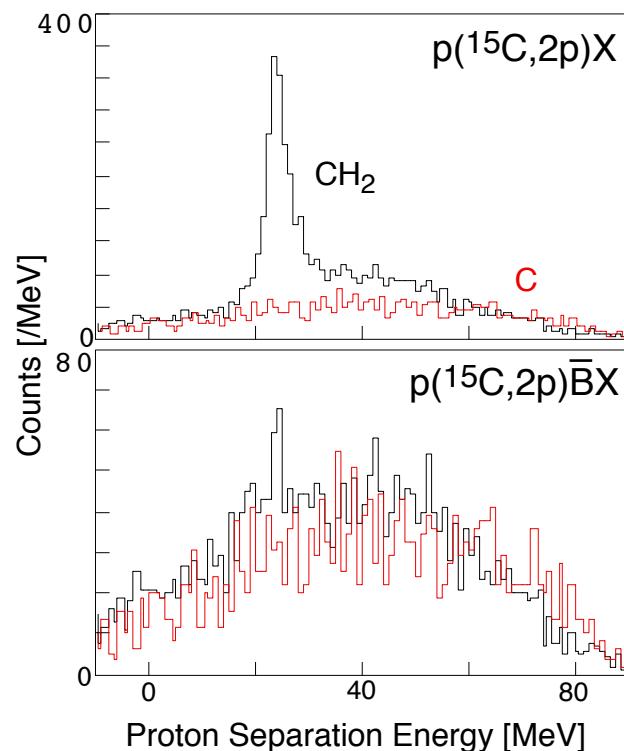
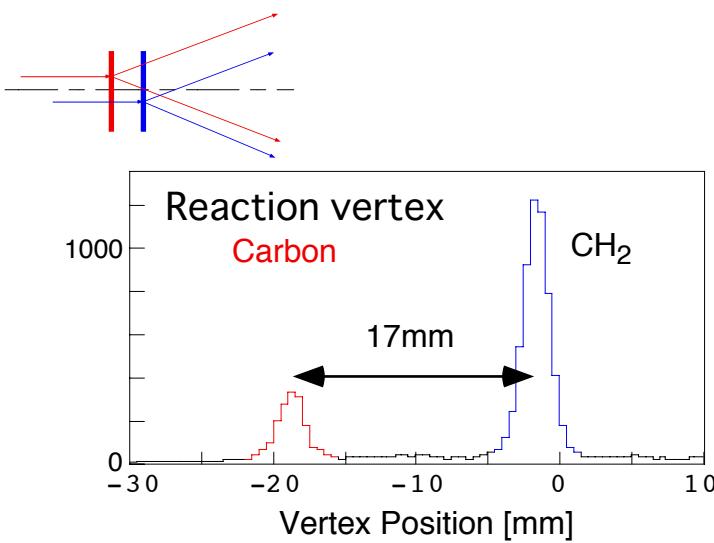


Solid Hydrogen Target (SHT)

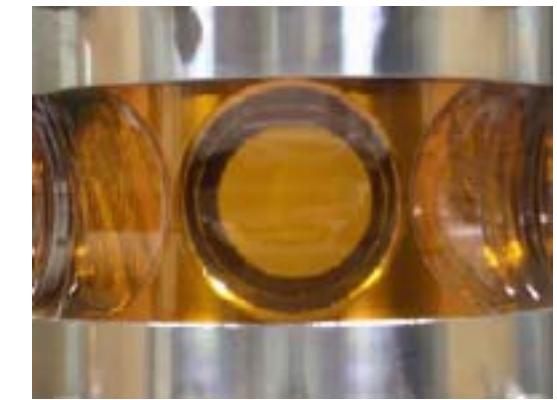
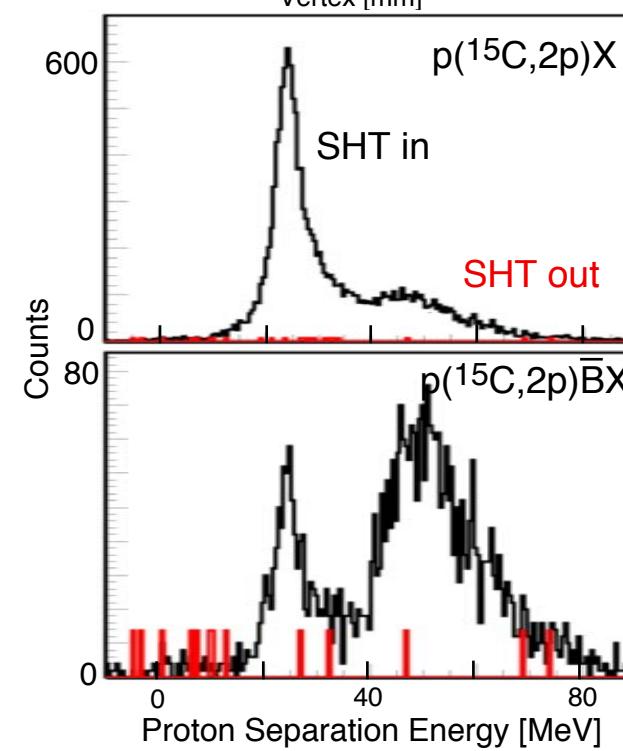
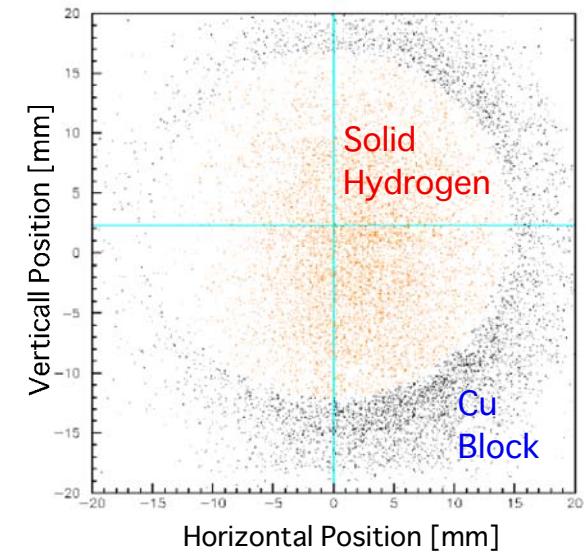
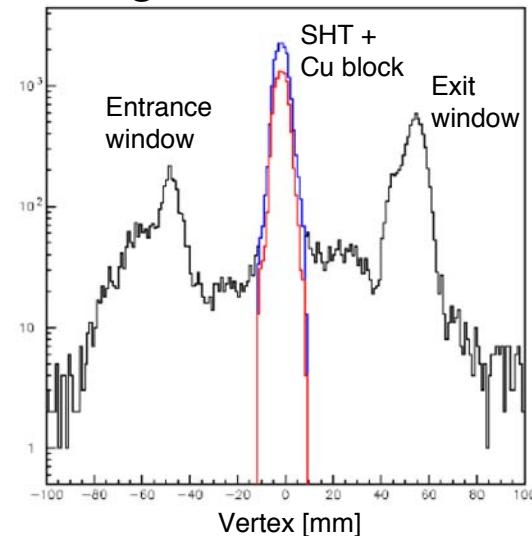


"Hydrogen" Target

- $\text{CH}_2(100\text{mg}/\text{cm}^2)$ -C($50\text{mg}/\text{cm}^2$)



- Solid Hydrogen : 30mm ϕ , 5mm t (W : 9 μm Mylar)
Target (SHT)



Target : 44 mg/cm²
thickness ~CH₂ 3mm
Vac window : 50 μm kapton

Measured Quantities

beam :

velocity (β) : $\sigma_\beta / \beta \approx 1.2 \times 10^{-3}$ "Symmetric" Geometry $\theta_{CM}(pp) \approx 90^\circ$

phase space : $\sigma \approx 1 \text{ mrad}$

two protons :

Angle : $\theta_{Lab} = \pm 39^\circ \pm 9^\circ (\text{H}, \text{V})$ $\sigma \approx 3 \text{ mrad}$

Energy : $T_p = 20 - 210 \text{ MeV}$ $\sigma_T / T \approx 1\% @ T_p = 115 \text{ MeV}$

forward particles :

(Z,A) identified: $\sigma_A \approx 0.25$



momentum (\vec{q}) : $\vec{q}_\perp = (\vec{p}_1 + \vec{p}_2)_\perp$

$$\vec{q}_\parallel = \frac{(\vec{p}_1 + \vec{p}_2)_\parallel}{\gamma} - \beta \left(M_A - M_{A-1} - \frac{q^2}{2M_{A-1}} \right)$$

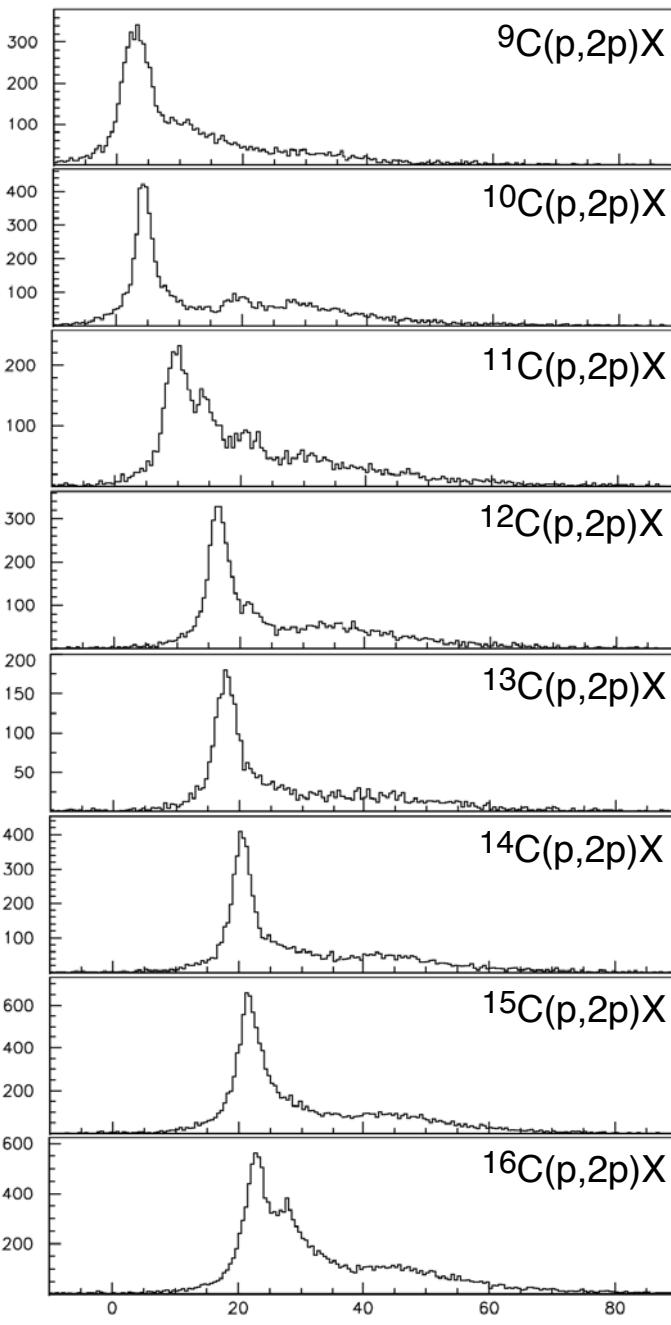
separation energy (S_p) :

$$S_p = \beta \gamma (\vec{p}_1 + \vec{p}_2)_\parallel - (\gamma - 1)m_p - \gamma(T_1 + T_2) - \frac{q^2}{2M_{A-1}}$$

+ acceptance correction

Proton-Separation-Energy (S_p) Distribution

Inclusive



$A-1B$ detected in FWD $\sim A-1B_{gr}$

$$\sigma(E_S) \sim 1.2-1.9 \text{ MeV}$$

p-hole

$10C(p,2p)2\alpha$

$11C(p,2p)^{10}B$

$12C(p,2p)^{11}B$

$13C(p,2p)^{12}B$

$14C(p,2p)^{13}B$

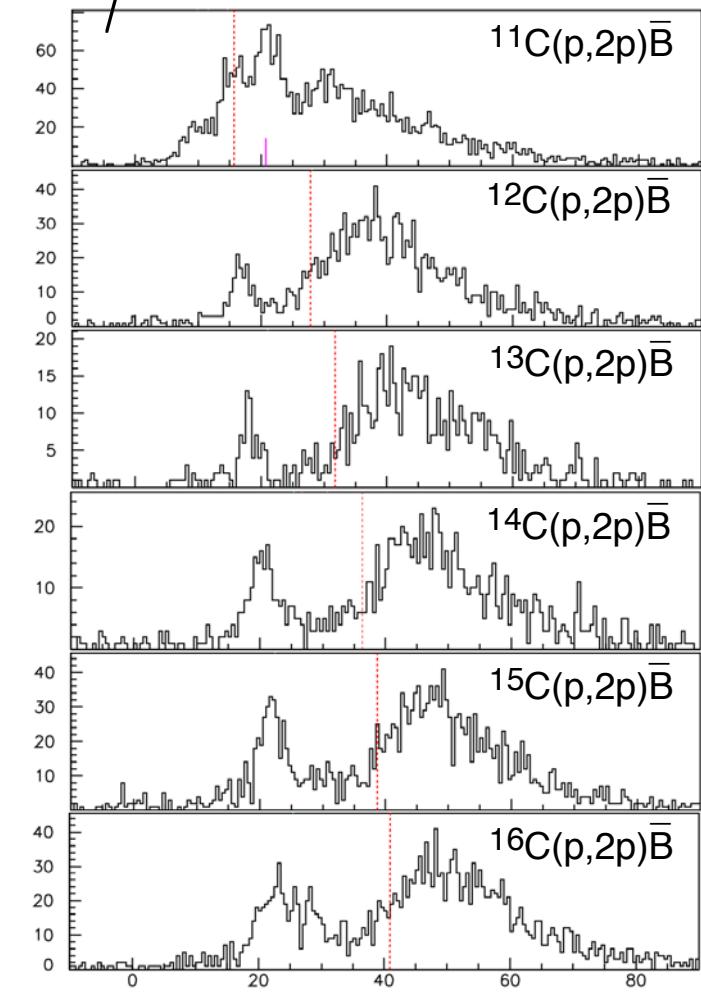
$15C(p,2p)^{14}B$

$16C(p,2p)^{15}B$

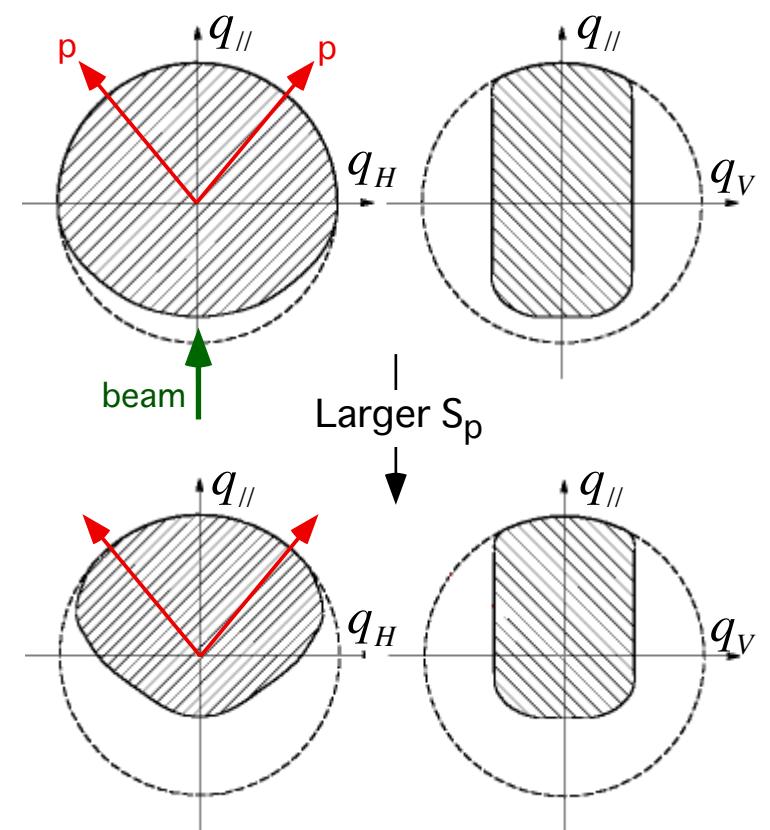
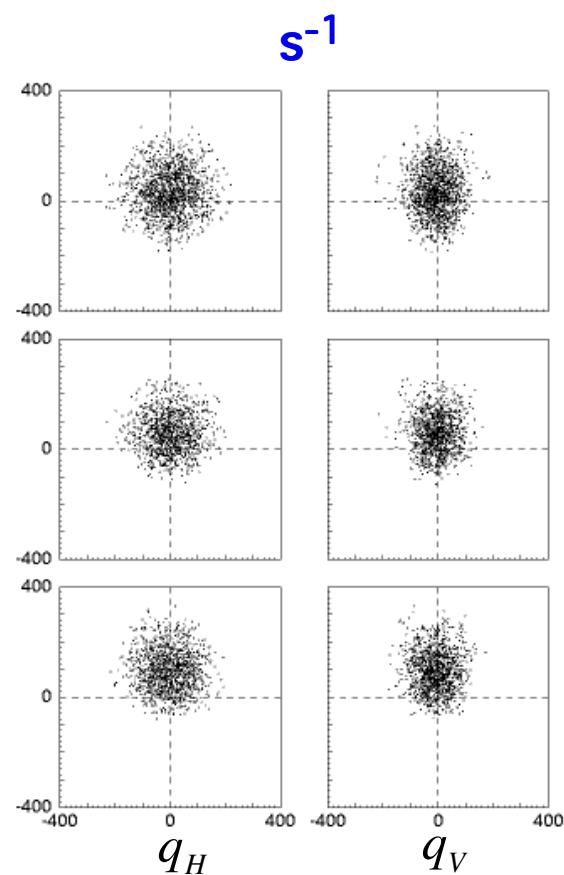
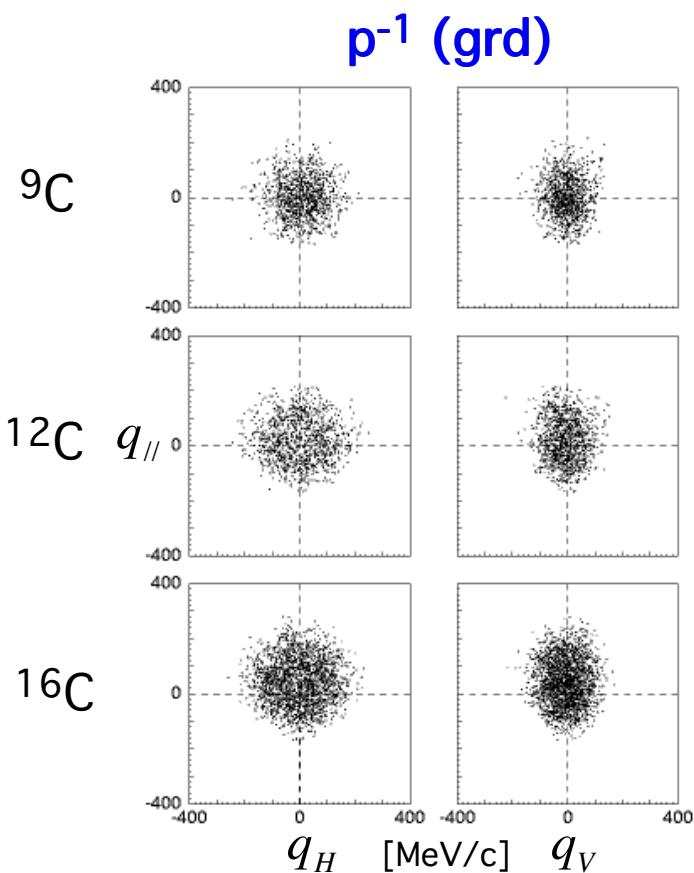
tagging $A-1B_{gr}$

tagging charged-particle decay
from $A-1B^*$ s-hole

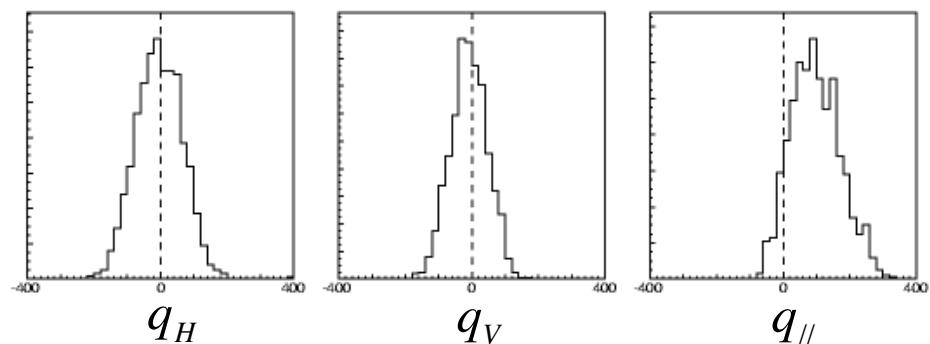
proton
threshold



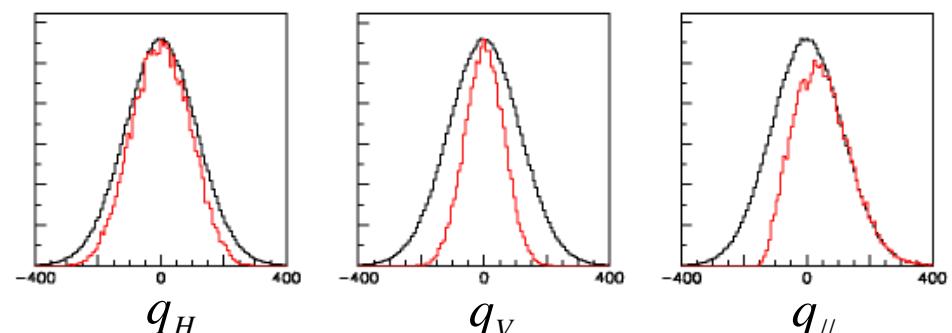
Effect of Angular Acceptance



16C data

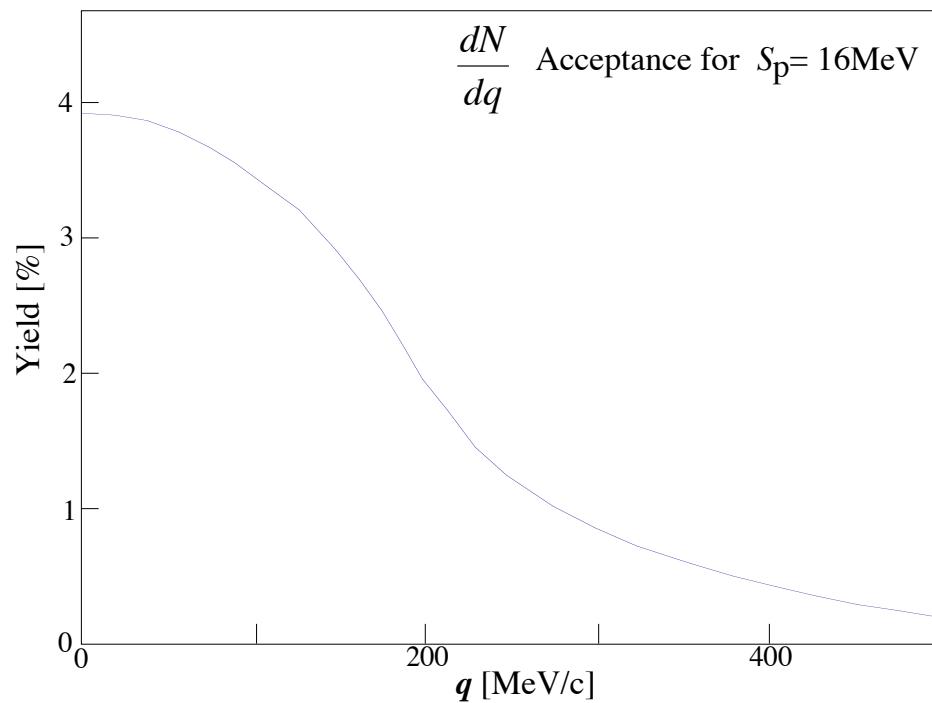


Simulation



Acceptance Correction (Simulation)

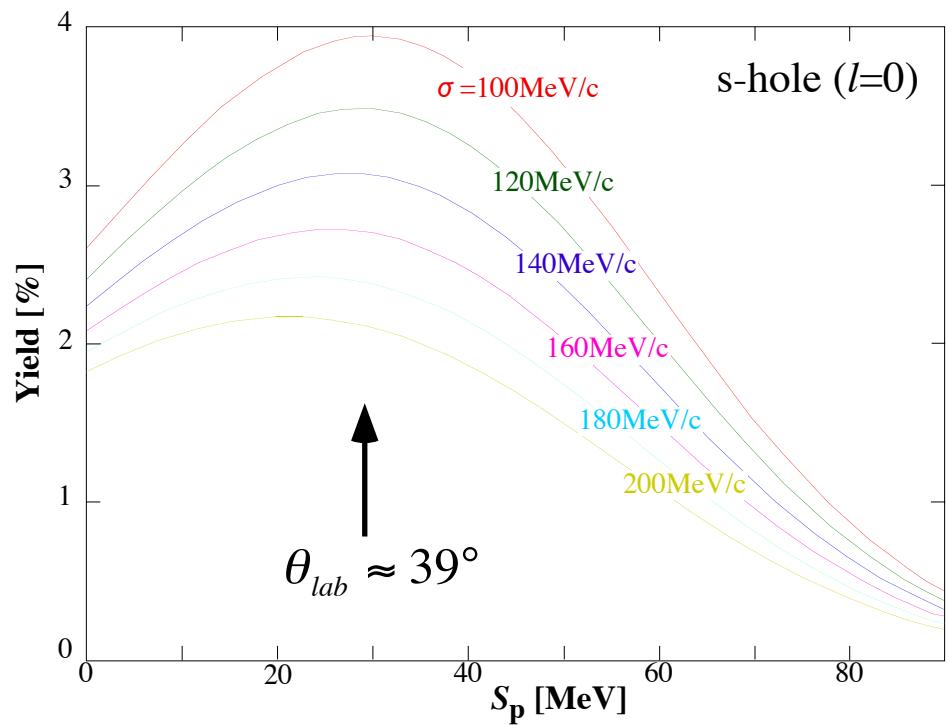
(1) Momentum distribution $\frac{dN}{dq}$



Assumption

- * p-p angular distribution isotropic in p-p CM

(2) Separation Energy distribution



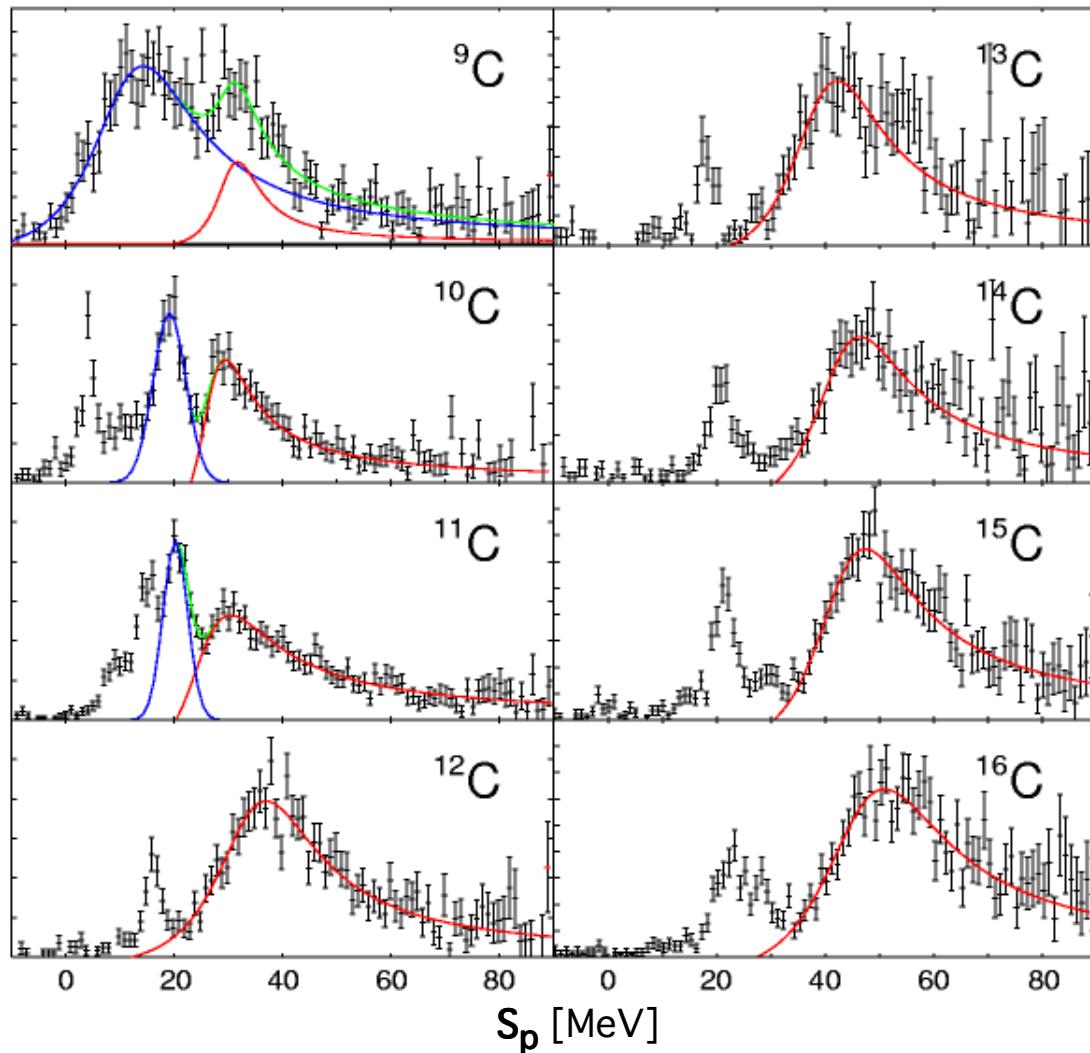
Assumption

- * p-p angular distribution isotropic in p-p CM
- * Momentum Distribution : Harmonic Osc.

$$\frac{d^3 N_l}{d\vec{q}^3} \propto \frac{d^3 N_l}{q^2 dq} \propto q^{2l} \exp\left(-\frac{q^2}{\sigma_l^2}\right)$$

S_p Distribution : s-hole states

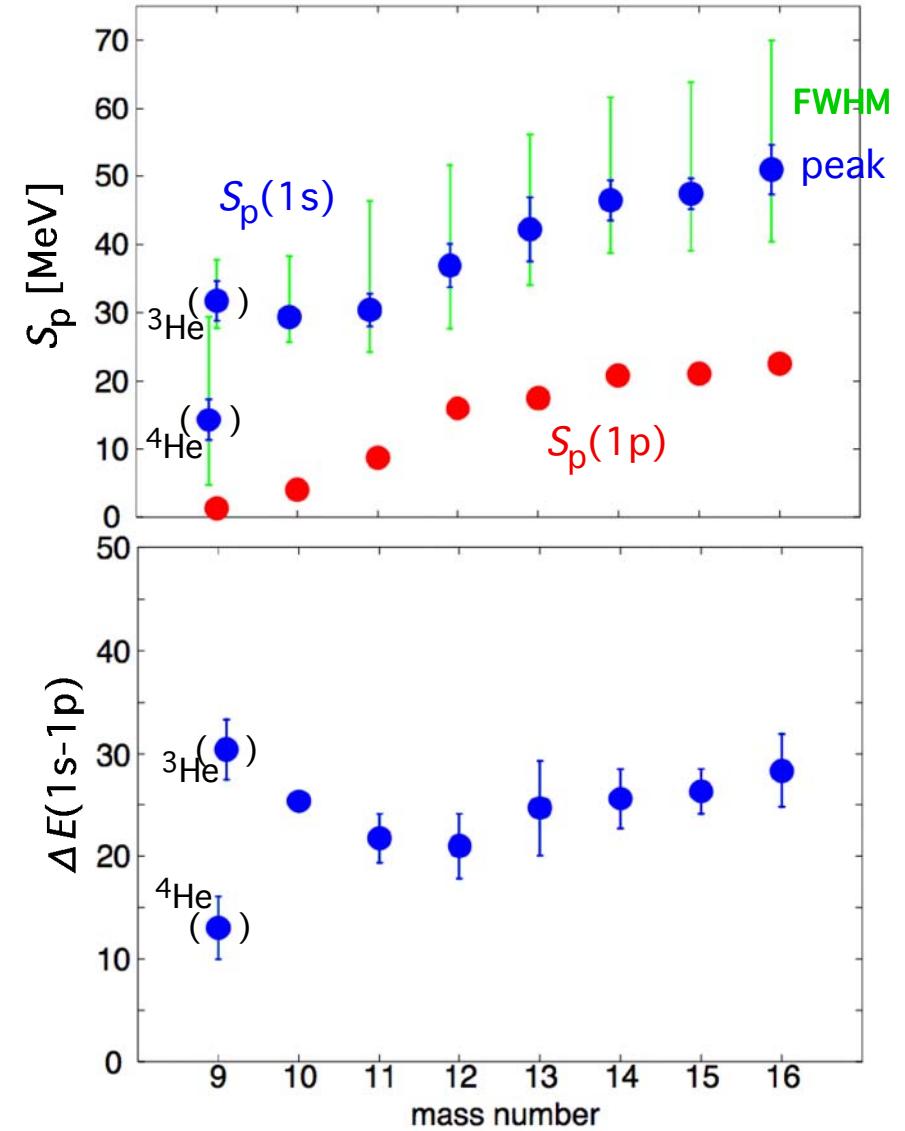
Systematic observation of s-hole states



Fitting:

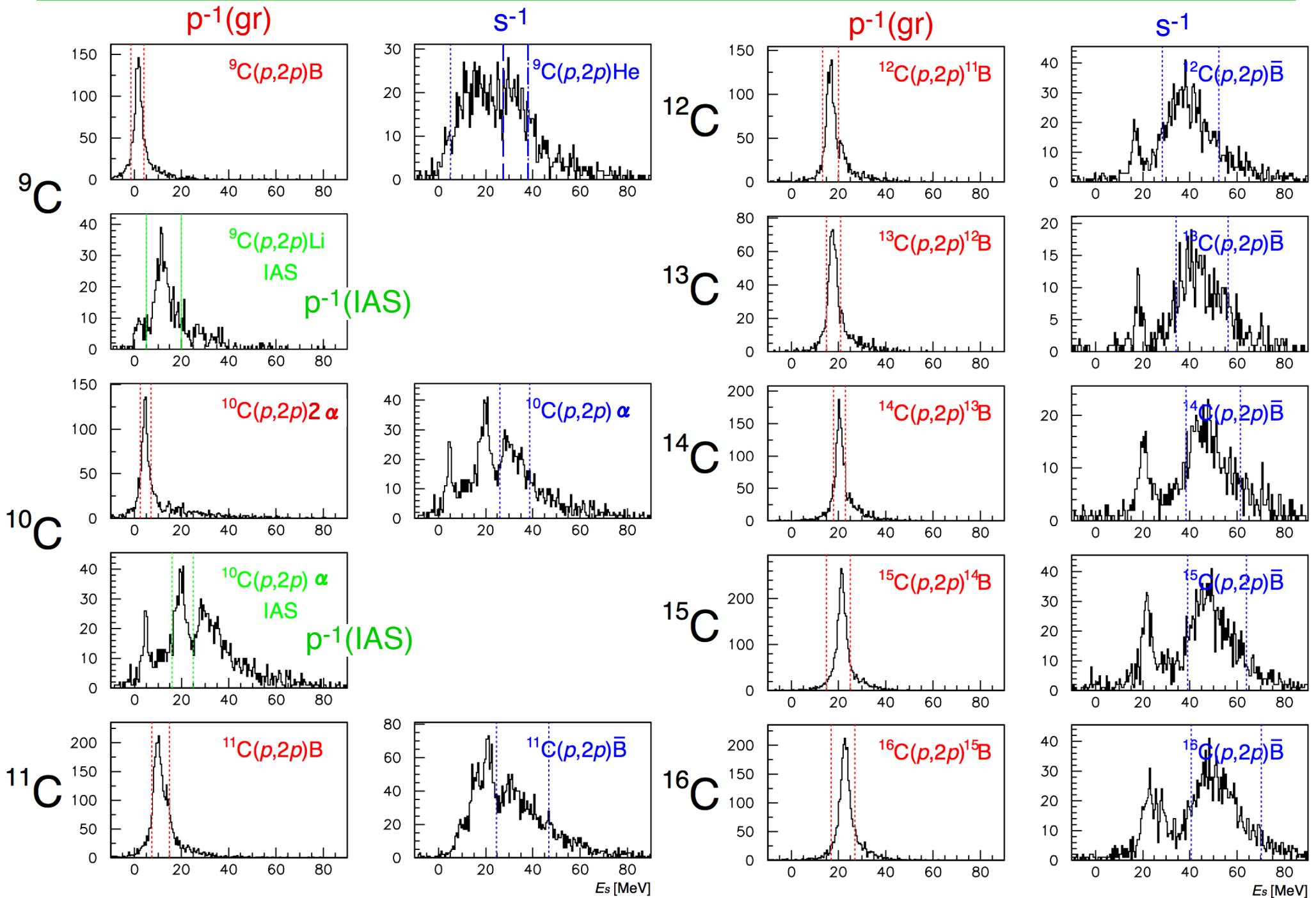
$$f(s_p) = \frac{s_p - a}{(s_p - b)^2 + c^2}$$

→ Peak
Width (FWHM)

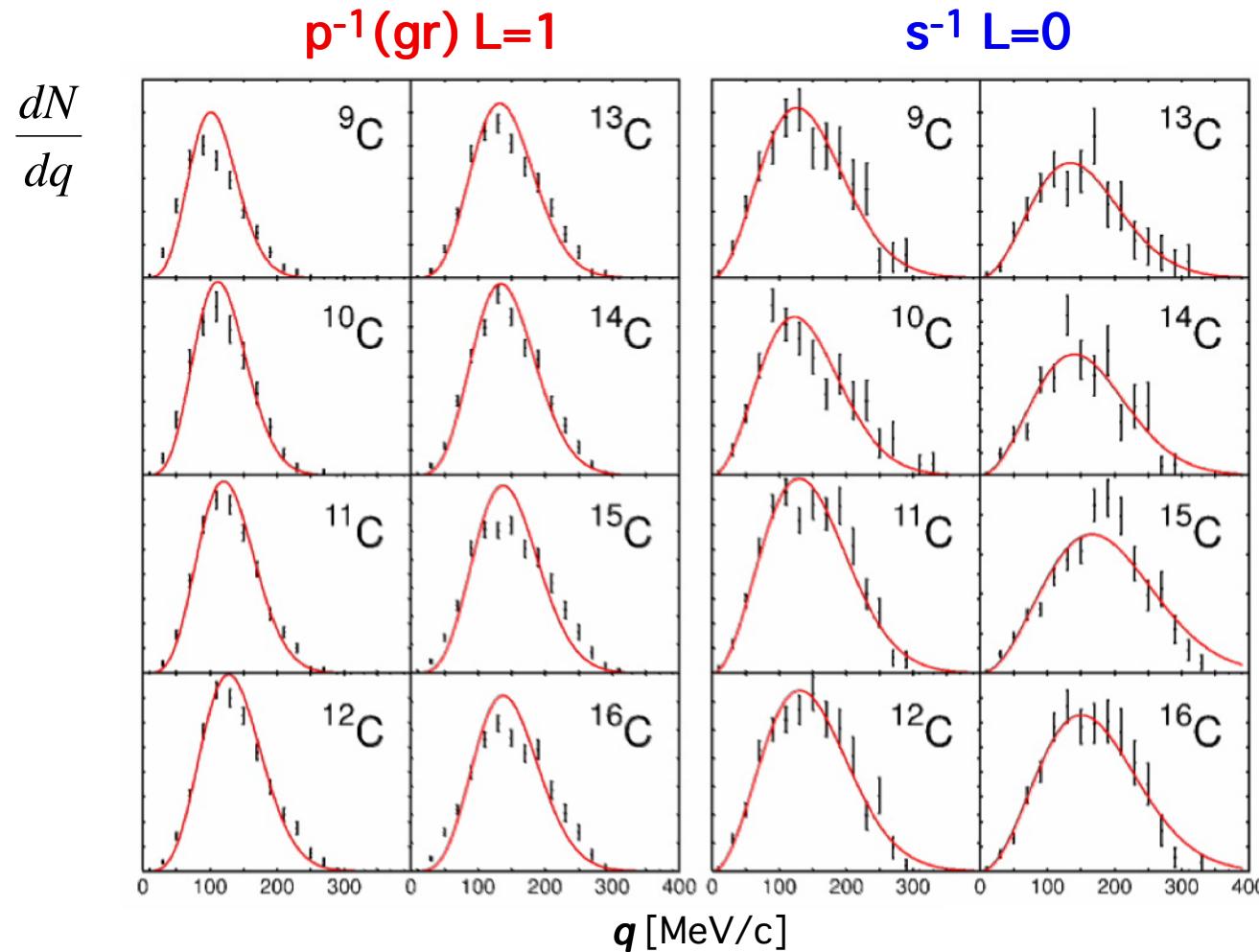


Energy gas widening on both sides

S_p selection for momentum distribution



Momentum Distribution

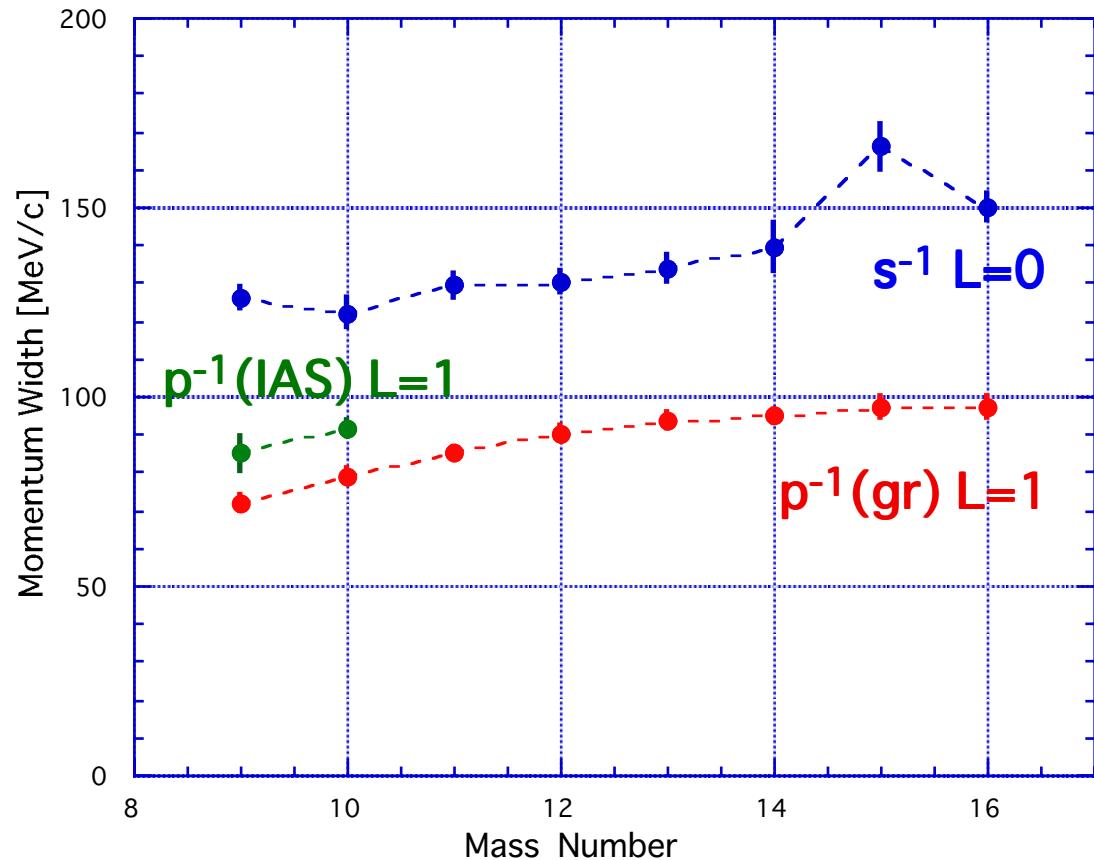


Fitting :
Harmonic Osc. shape

$$\frac{d^3 N_l}{dq} \propto q^{2l+2} \exp\left(-\frac{q^2}{\sigma_l^2}\right)$$

→ σ_0 s-hole $L=0$
 σ_1 p-hole (gr) $L=1$

Width of Momentum Distribution



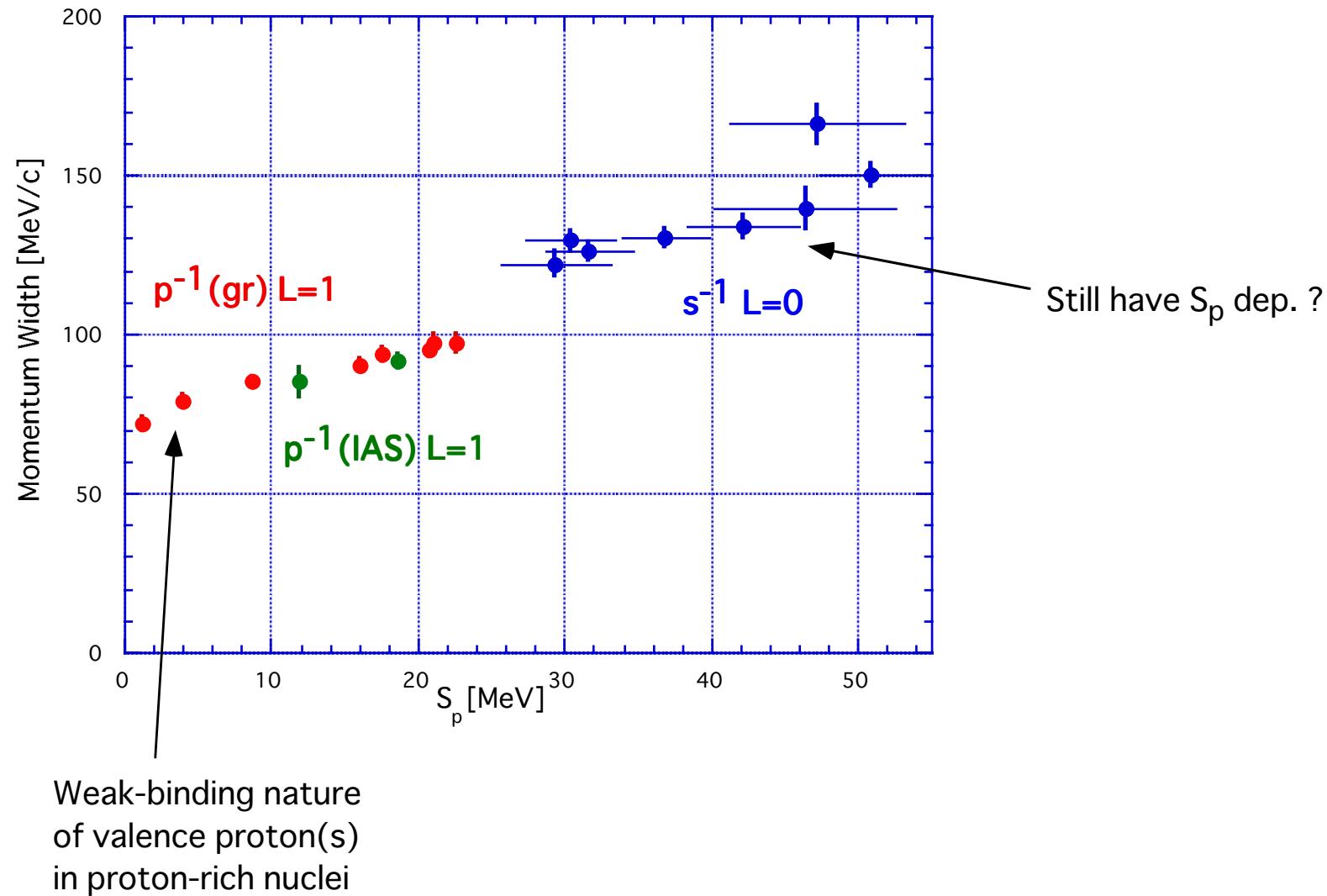
Width $\sigma_0(s), \sigma_1(p)$
Harmonic Osc. shape

$$\frac{d^3 N_l}{d\vec{q}^3} \propto q^{2l} \exp\left(-\frac{q^2}{\sigma_l^2}\right)$$

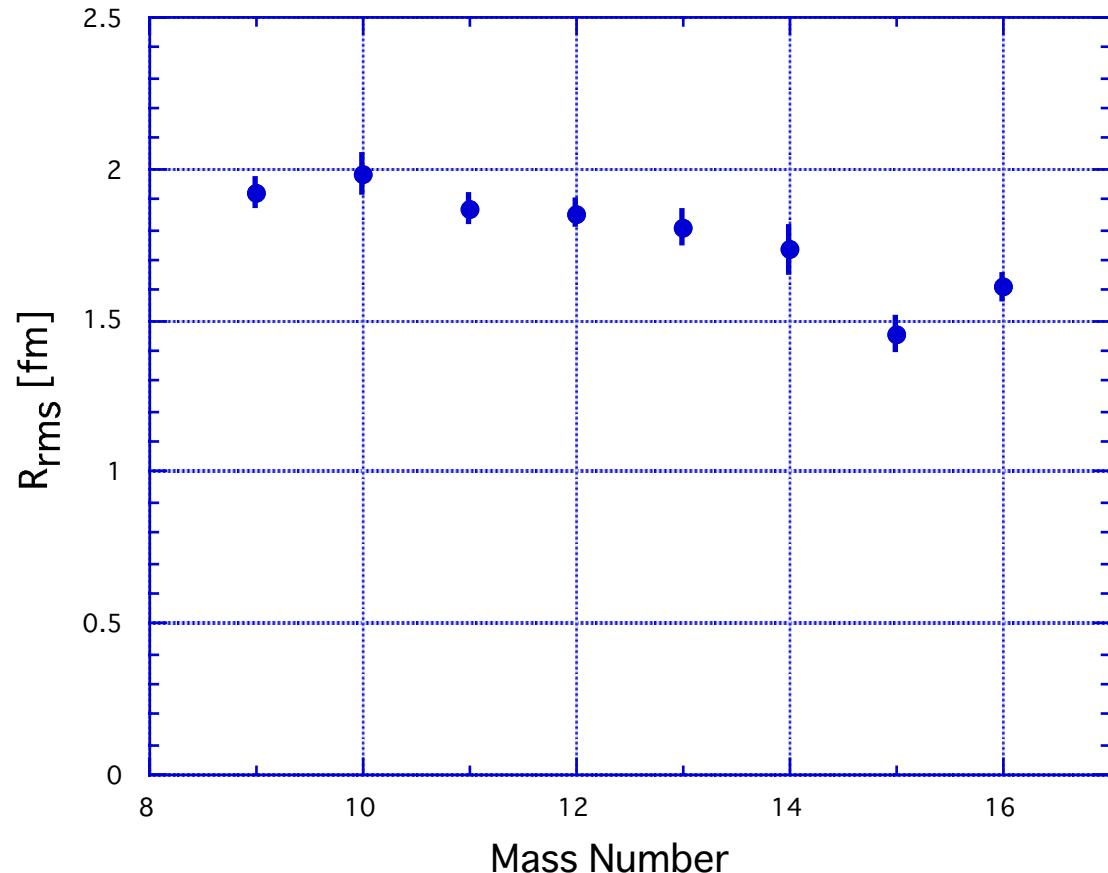
p^{-1} : width increases as S_p becomes larger

$s-1$: width increases toward neutron-rich side

Momentum Width : Separation-Energy Dep.



Rms Radius of $\pi 1s_{1/2}$ Orbit



Assuming Harmonic Oscillator :

$$R_{rms}^{1s} = \sqrt{\frac{3}{2}} \frac{\hbar c}{\sigma_s}$$

smaller towards neutron-rich side (shirinking)

Total (p,2p) Yield

Total (p,2p) Yield \propto Effective proton number (spectroscopic factor)

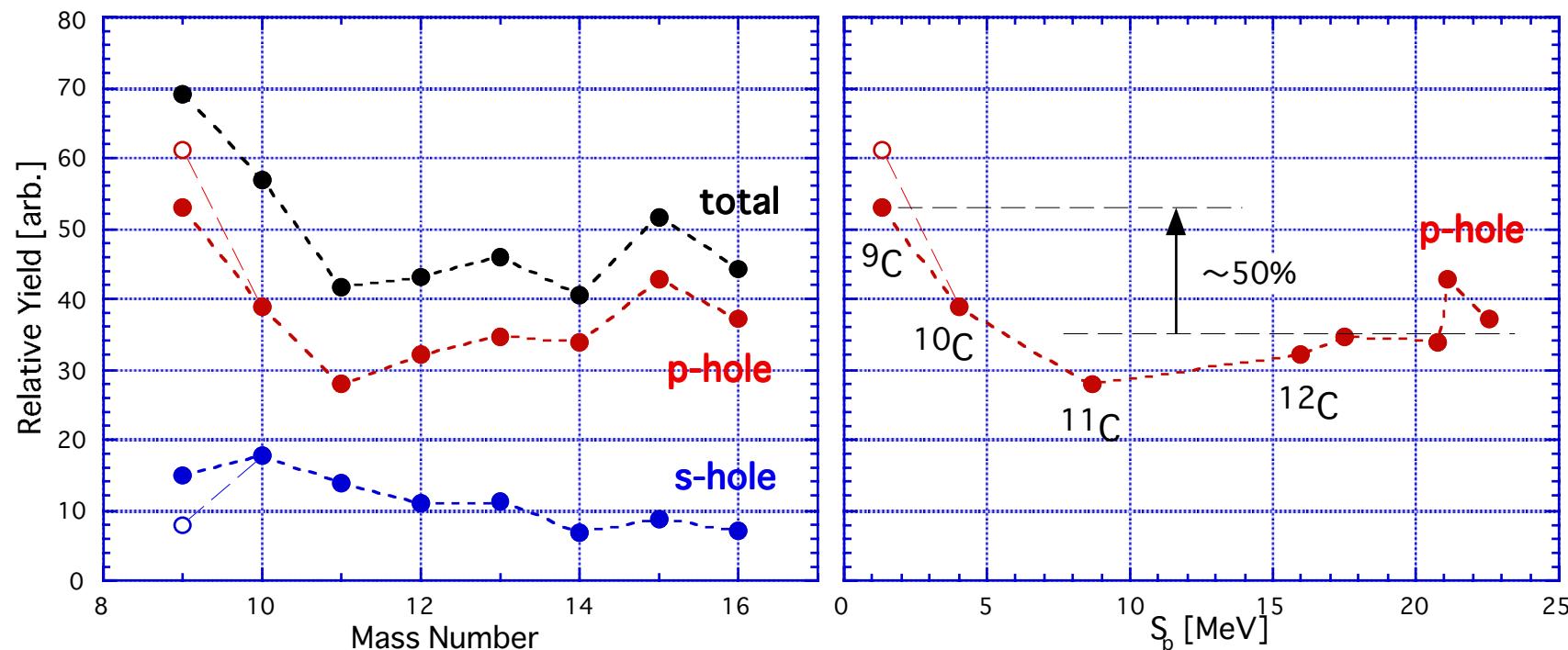
Separation of "p-hole" & "s-hole" :

p-hole : $p(C,2p)Bx$

+ acceptance correction

s-hole : $p(C,2p)\bar{B}x$ & $S_p >$ proton threshold

Isotropic in pp CM & Harmonic Osc.



${}^9\text{C}$ ($S_p=1.3\text{MeV}$)

Yield from p shell is about 50% larger
effective proton number/spectroscopic factor larger

Summary

${}^9-{}^{16}\text{C}(\text{p},2\text{p}){}^{8-15}\text{B}$ proton knockout reactions @250 MeV/A were measured for systematic information of weakly to strongly-bound valence protons(1p) deeply-bound inner-shell protons(1s)

(1) separation-energy distribution

momentum distribution : measured

total (p,2p) yield

decay mode tagged : p-hole/s-hole states separated

(2) Valence shell ($1\text{p}_{3/2}$) orbit : $S_{\text{p}}=1.3-23\text{MeV}$

- momentum distribution :

quantitatively consistent with simple calculation, adjusting S_{p}

- total (p,2p) yield :

${}^9\text{C}$ ($S_{\text{p}}=1.3\text{MeV}$) yield is larger by about 50%

effective proton number/spectroscopic factor is larger

(3) Inner shell ($1\text{s}_{1/2}$) orbit : $S_{\text{p}}=30-50\text{MeV}$

- s-hole states observed systematically

- energy gap $\Delta E(s_{1/2}-p_{3/2})$

minimum around ${}^{12}\text{C}$, wider on both sides

- charge rms radii of s-orbit(core)

shirinks from $\sim 2\text{fm}$ to $\sim 1.5\text{fm}$ between ${}^9\text{C}$ and ${}^{16}\text{C}$