

Low-energy tests of the CVC-hypothesis and the unitarity of the CKM-matrix by means of precision mass measurements in a Penning trap

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Physics of superallowed beta decay

Conserved vector current hypothesis:
 ft should be constant

$$Ft \equiv ft(1 + \delta_R)[1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2(1 + \Delta_R)}$$

- δ_R radiative correction
 $f(Z, Q_{EC}) \sim 1.5\%$
- $\delta_C - \delta_{NC}$ isospin symmetry breaking correction
 $f(\text{nuclear structure}), 0.3-0.7\%$
- Δ_R nucleus-independent radiative correction
 $f(\text{interactions}), \sim 2.4\%$

Exp. parameters to be determined:

Beta decay half-life $T_{1/2}$
 Beta decay branching ratio I_b
 Decay energy Q_{EC}

Single nucleus: determination of $G_V^2(1 + \Delta_R)$

Many transitions: Check if Ft is constant
 → Test of the CVC

One can deduce V_{ud} by
 combining beta decay and
 muon decay data

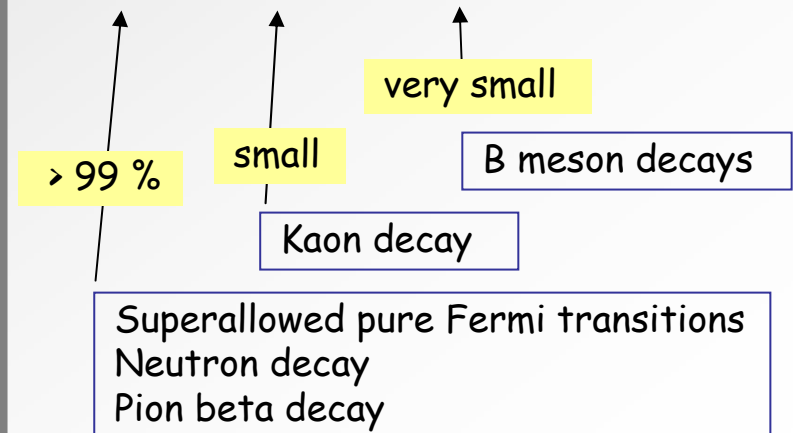
$$V_{ud}^2 = \frac{G_V^2}{G_\mu^2}$$

Cabibbo-Kobayashi-Maskawa quark
 mixing matrix:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Unitarity test of CKM-matrix

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$



World data 2005

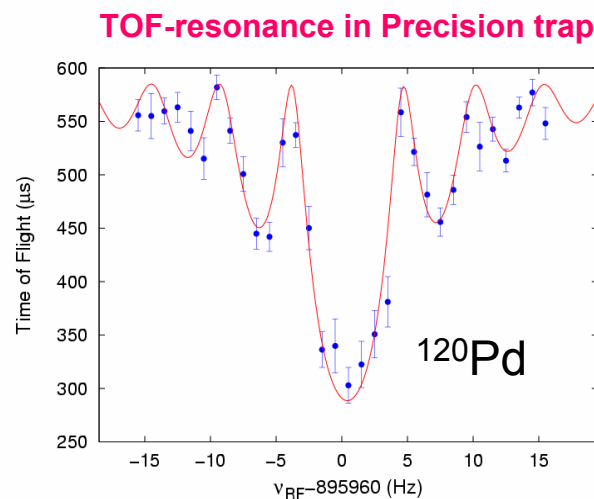
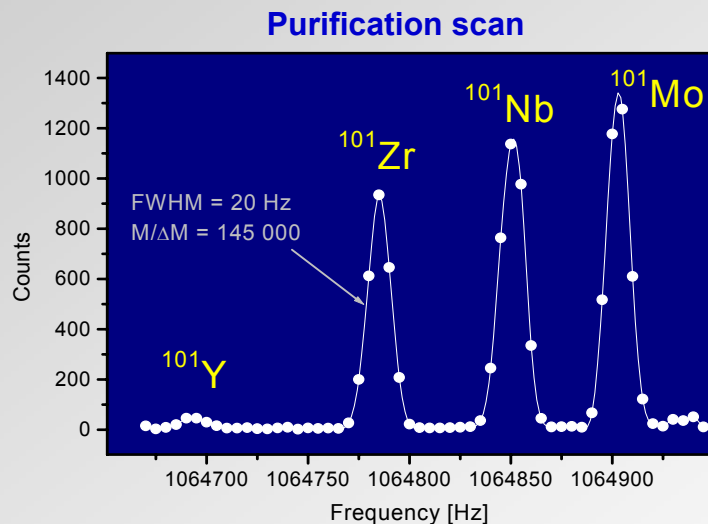
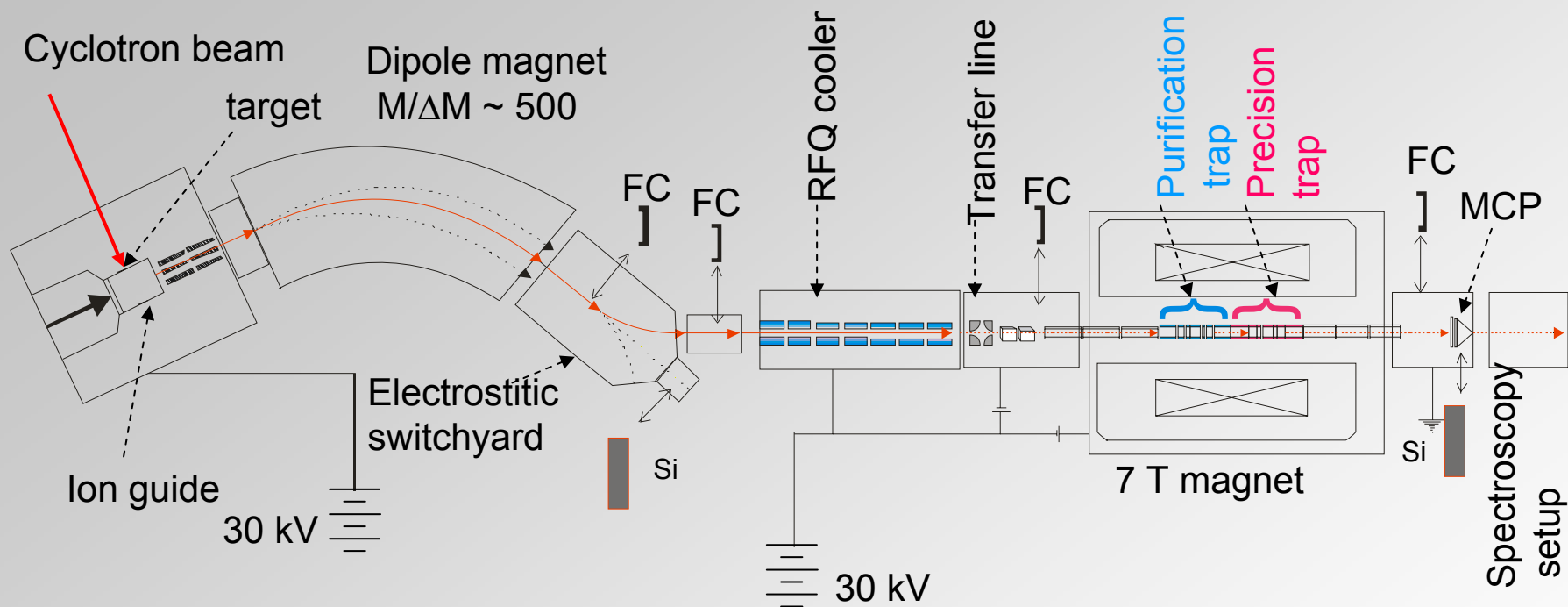
J. Hardy and I. Towner, Phys. Rev. C 71 (2005) 055501

- o Nine best known cases: ^{10}C , ^{14}O , $^{26}\text{Al}^{\text{m}}$, ^{34}Cl , $^{38}\text{K}^{\text{m}}$, ^{42}Sc , ^{46}V , ^{50}Mn , and ^{54}Co
(ft value known to a precision of $\sim 0.1\%$)
- o Together with new data on ^{22}Mg , ^{34}Ar and ^{74}Rb
(ft value known to a precision $< 0.40\%$)
- o The average Ft from survey: $\boxed{\text{Ft} = 3072.7(8)} \rightarrow \boxed{3073.5(12)}$ δ_c from OB or TH
- o G_V constant verified to 0.013%
- o Precise value determined for $\boxed{V_{ud} = G_V/G_\mu = 0.9738(4)}$
- o Unitarity of the CKM-matrix $\boxed{|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9966 \pm 0.0014}$

NEW TRENDS:

- o Improve the precision of the nine cases
- o Add new cases with larger corrections $\rightarrow$ to test corrections and improve them
- o New cases with $A=18-42$ ($T_z=-1$)
- o New cases with $A \geq 62$ ($T_z=0$)

JYFLTRAP at IGISOL-facility



Basic equations for mass determination

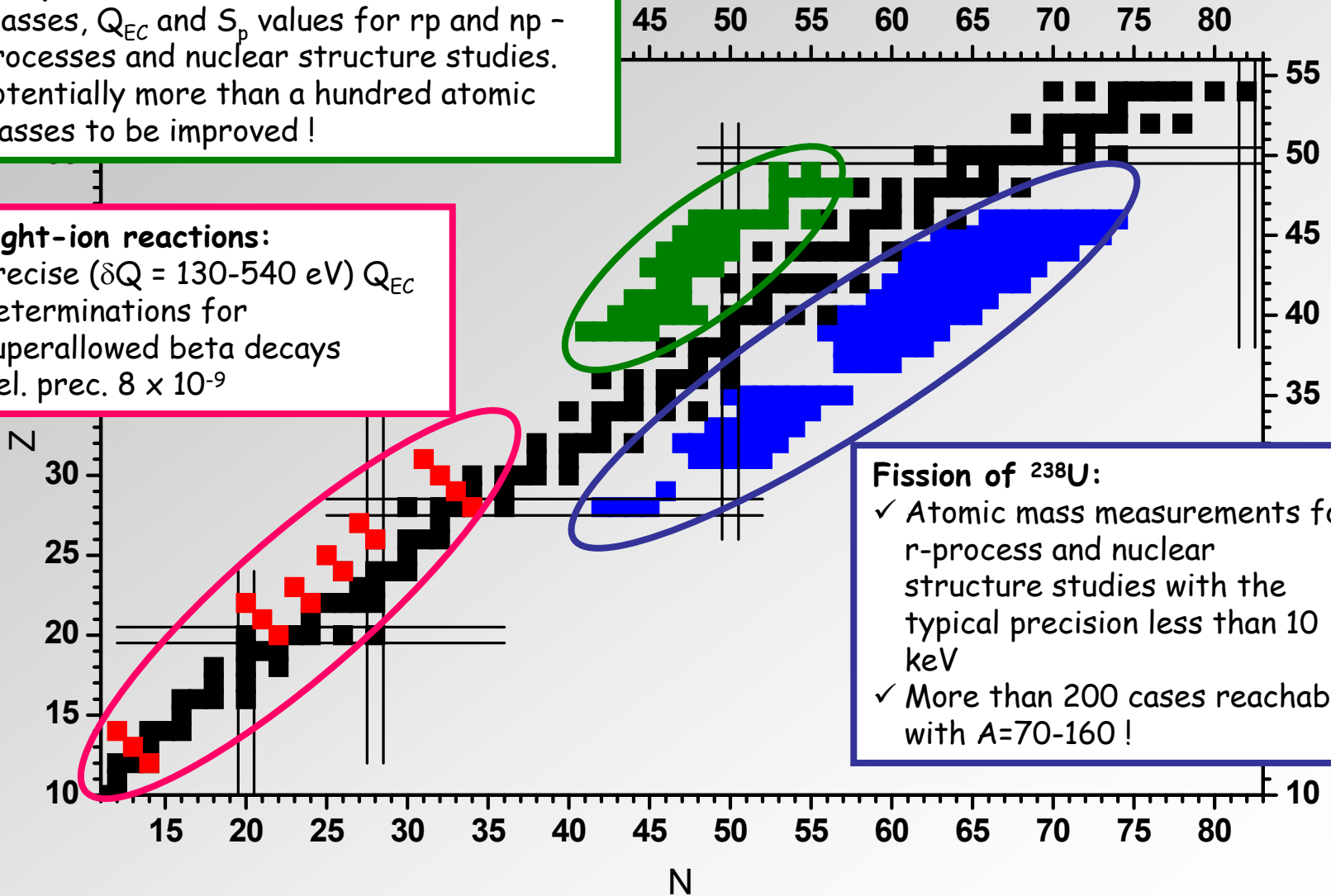
$$f_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

$$\frac{f_{c,\text{ref}}}{f_c} = \frac{m - m_e}{m_{\text{ref}} - m_e}$$

Overview of JYFLTRAP mass program

HI, p- and ^3He -induced reactions:
Masses, Q_{EC} and S_{p} values for rp and np - processes and nuclear structure studies. Potentially more than a hundred atomic masses to be improved !

Light-ion reactions:
Precise ($\delta Q = 130\text{-}540\text{ eV}$) Q_{EC} determinations for superallowed beta decays
Rel. prec. 8×10^{-9}



Fission of ^{238}U :

- ✓ Atomic mass measurements for r-process and nuclear structure studies with the typical precision less than 10 keV
- ✓ More than 200 cases reachable with $A=70\text{-}160$!

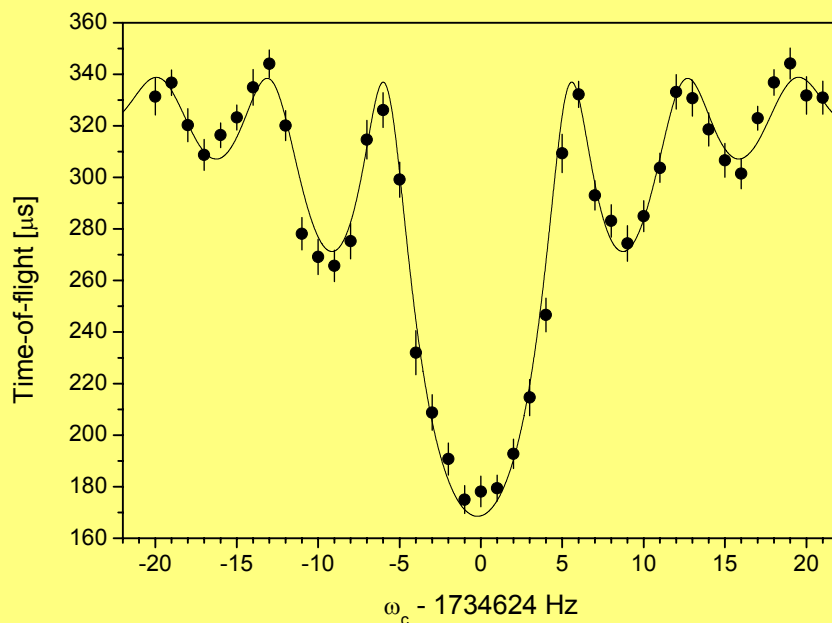
^{62}Ga - extension to higher Z

JYFLTRAP:

- ✓ 48 MeV p-beam on ^{64}Zn -target
- ✓ 600 ions/s ^{62}Ga , 7×10^5 ions/s ^{62}Zn
- ✓ Direct comparison between mother and daughter isotopes

$$Q_{EC} = M_p - M_d = \underbrace{\left(\frac{f_d}{f_p} - 1 \right)}_{\leq 10^{-3}} M_d \rightarrow \Delta M_d \text{ negligible !}$$

- ✓ $Q_{EC} = 9181.07(54) \text{ keV}$
- ✓ Rel. mass precision 1.8×10^{-8}
- ✓ Additional check for ^{62}Ni and ^{62}Cu



TRIUMF:

High precision branching ratio measurement:
B. Hyland et al., PRL 97 (2006) 102501

19 gamma-rays $\rightarrow$ superallowed
branching ratio 99.861(11) %

$\rightarrow ft = 3075.6(14) \text{ s}$ (purely experimental)

$Q_{EC} = 9181.07(54) \text{ keV}$
 $T_{1/2} = 116.175(38) \text{ ms}$
 $I_b = 99.861(11) \%$
Uncertainty of $(\delta_{NS} - \delta_C)$ dominates

Deduced $\delta_C = 1.47(+0.13)(-0.18)$

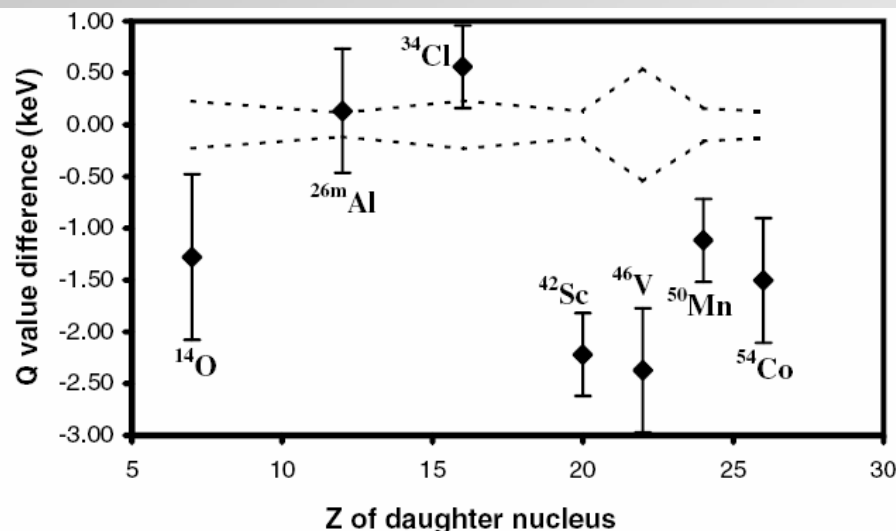
Towner&Hardy: 1.38(16)
Sagawa: 1.42
Ormand-Brown: 1.30/1.69
(HF)/(WS)

Q_{EC} -values of $^{26}\text{Al}^m$, ^{42}Sc and ^{46}V

Canadian Penning Trap at Argonne:

G. Savard et al., Phys. Rev. Lett. 95 (2005) 102501

- $Q_{EC}(^{46}\text{V}) = 7052.90(40)$ keV, which differed by 2.19 keV from the previous compilation
- Detailed analysis of the existing new data against earlier data
- Data set of H. Vonach et al., [Nucl. Phys. A278 (1977) 189], which affects 7 of the best nine cases was found to be systematically off compared to other measurements



"Penning trap revolution ?!"
(W. Marciano, NUPAC at CERN, Nov-2005)

JYFLTRAP:

$^{46}\text{Ti}(p,n)^{46}\text{V}$, $E(p) = 20$ MeV

$^{26}\text{Mg}(p,n)^{26}\text{Al}$, $E(p) = 15$ MeV

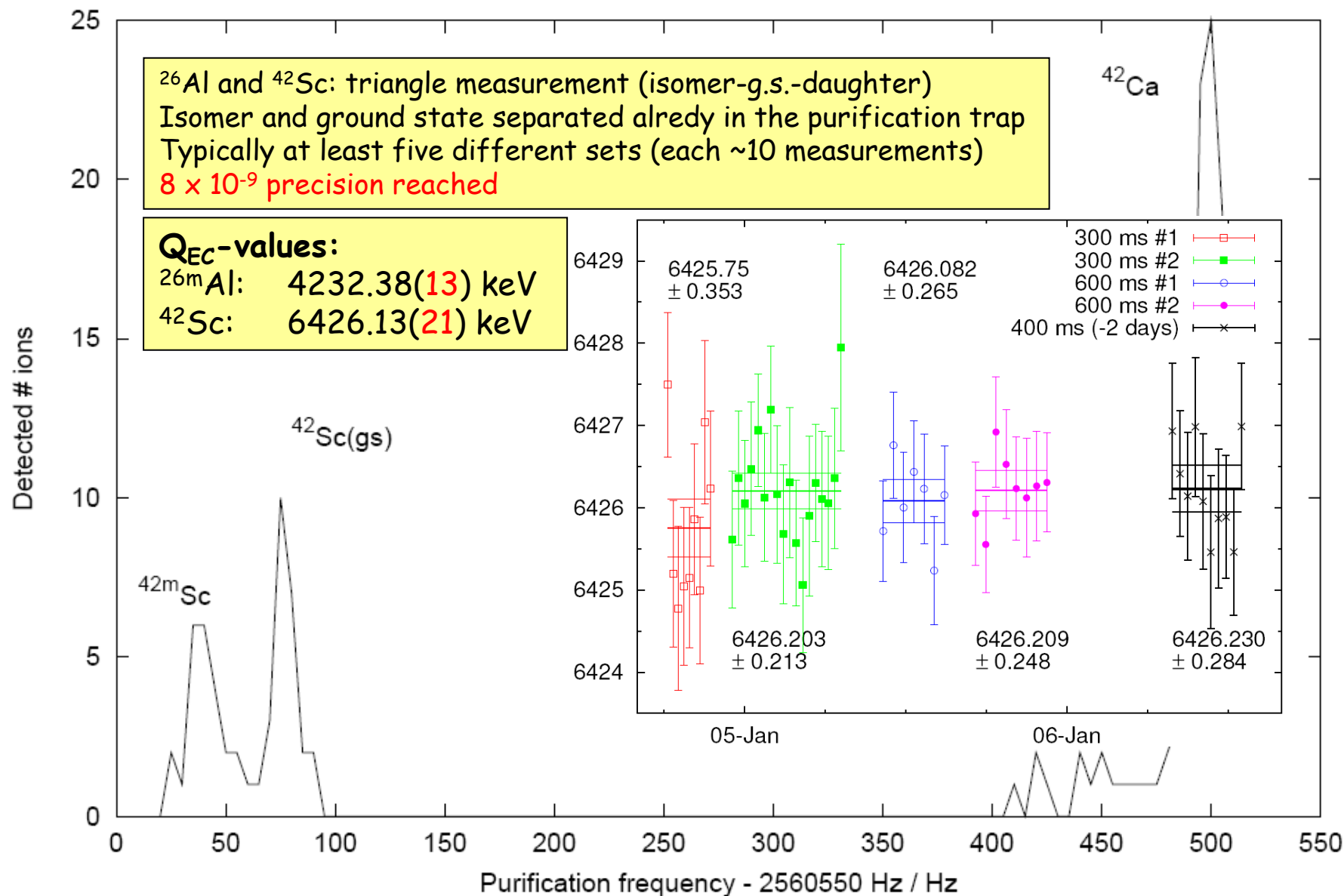
$^{40}\text{Ca}(^3\text{He},p)^{42}\text{Sc}$, $E(^3\text{He}) = 20$ MeV

Conclusions:

- ✓ $Q_{EC}(^{46}\text{V}) = 7052.72(31)$ keV in agreement with CPT
- ✓ Anomalous Q_{EC} -value of ^{46}V measured by G. Savard et al., was confirmed

T. Eronen et al., PRL97 (2006) 232501

Consistency checks: $^{26}\text{Al}^m$ and ^{42}Sc

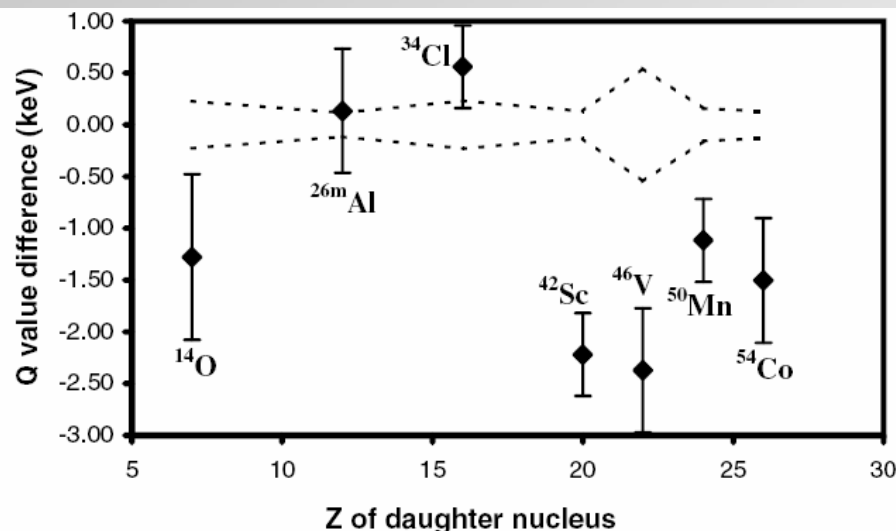


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- ✓ Anomalous Q_{EC} -value of ^{46}V measured by G. Savard et al., was confirmed
- ✓ Extended systematic deviation between reaction data and PT measurements is ruled out in 100 eV limit.
- ✓ There is no significant change in V_{ud} value
 - ✓ $V_{ud}(\text{new}) = 0.9737(3)$
 - ✓ $V_{ud}(\text{old}) = 0.9738(4)$

T. Eronen et al., PRL97 (2006) 232501

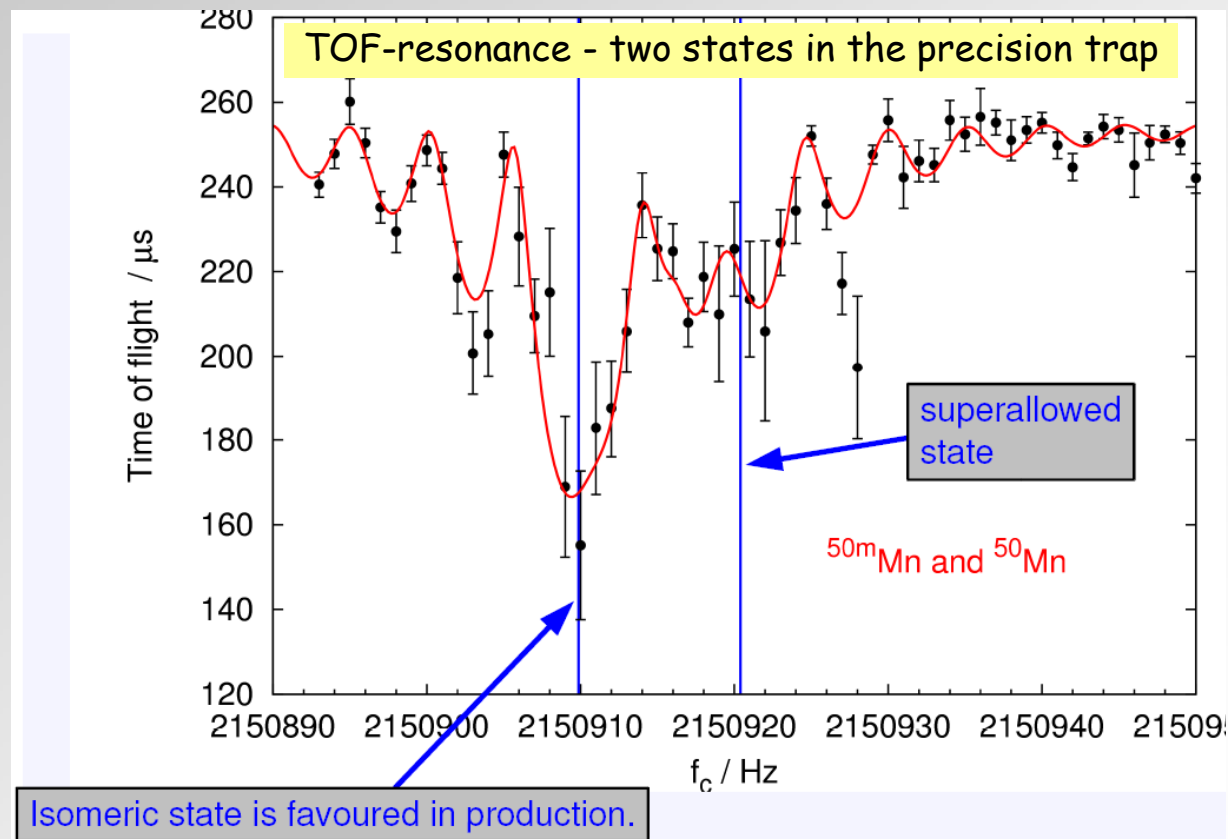
Further studies and challenges ...

^{50}Mn and ^{54}Co Q_{EC} -values, measured last week at JYFLTRAP

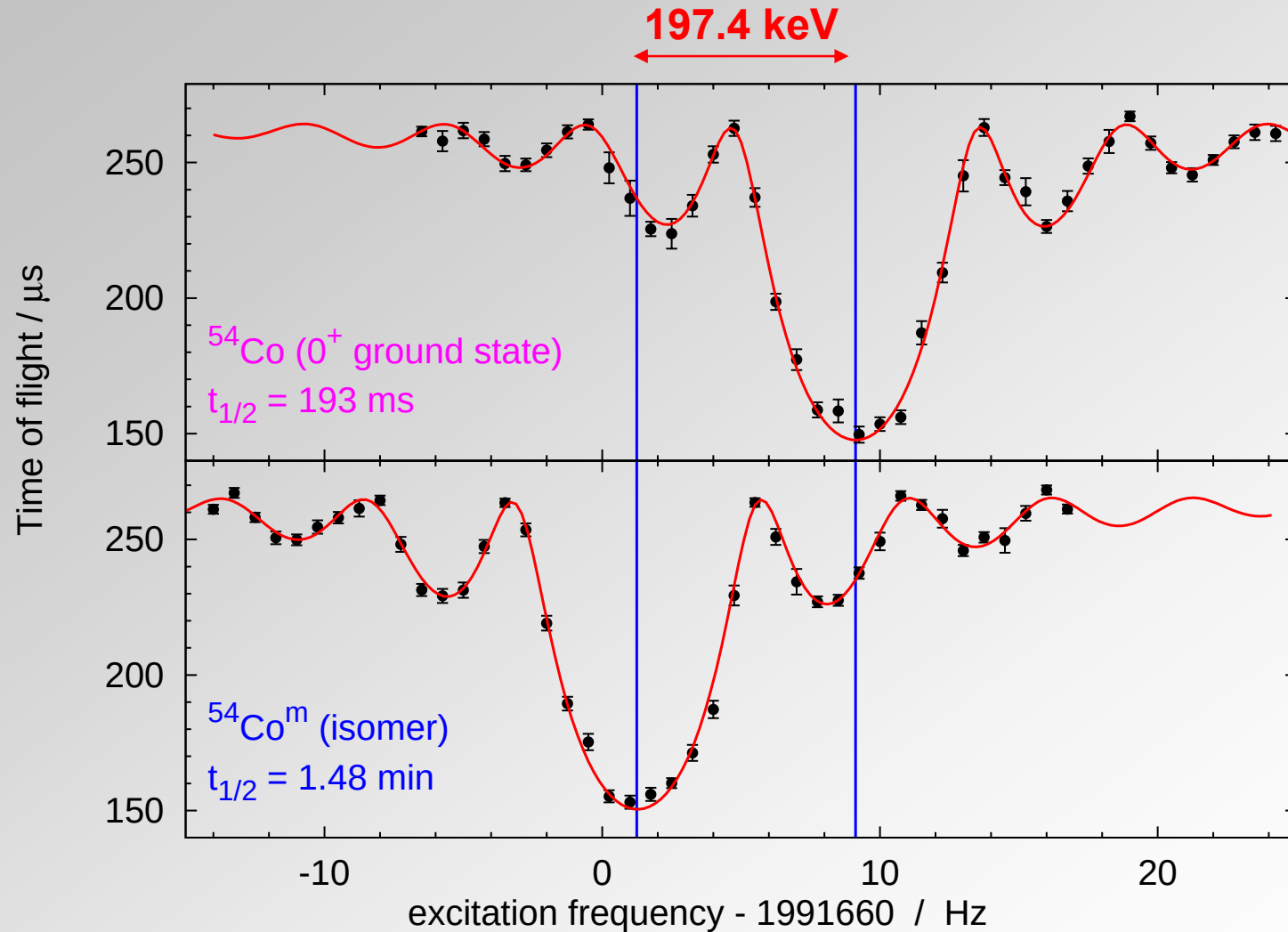
Both isomeric and ground state populated

$\Delta E(\text{g.s.-m})$ small and $T_{1/2}$ short

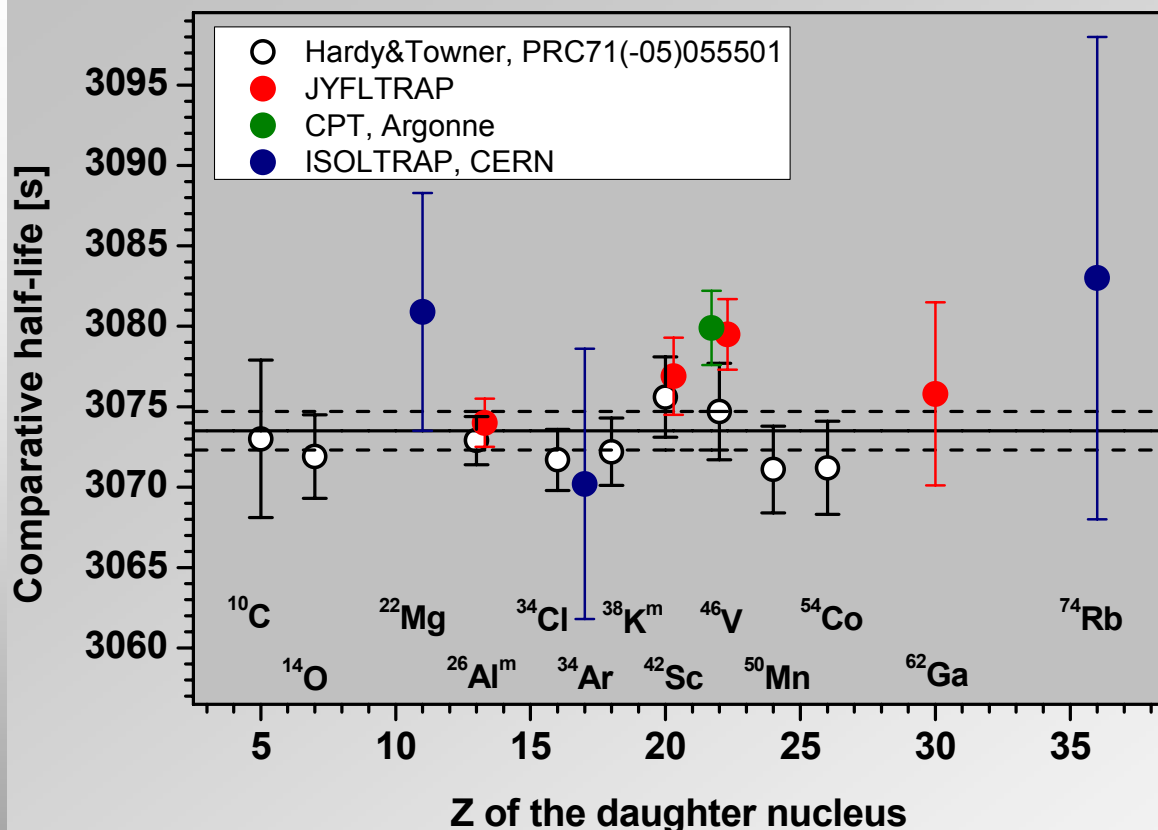
→ conventional isobaric purification does not work → Ramsey cleaning



Ramsey cleaning at work



Experimental status June-2007



New Q_{EC} -value determinations (Penning Trap):

²² Mg	M. Mukherjee <i>et al.</i> , Phys. Rev. Lett. 93 (2004) 150801
²⁶ Al ^m , ⁴² Sc, ⁴⁶ V	T. Eronen <i>et al.</i> , Phys. Rev. Lett. 97 (2006) 232501
³⁴ Ar	F. Herfurth <i>et al.</i> , Eur. Phys. J. A 15 (2002) 17
³⁸ Ca	G. Bollen <i>et al.</i> , Phys. Rev. Lett. 96 (2006) 152501
	S. George <i>et al.</i> , Phys. Rev. Lett. 98 (2007) 162501
⁴⁶ V	G. Savard <i>et al.</i> , Phys. Rev. Lett. 95 (2005) 102501
⁶² Ga	T. Eronen <i>et al.</i> , Phys. Lett. B 636 (2006) 191
⁷⁴ Rb	A. Kellerbauer <i>et al.</i> , Phys. Rev. Lett. 93 (2004) 072502

²²Mg, ³⁴Ar, ⁶²Ga and ⁷⁴Rb:
Error bars in Ft dos not
reflect the accuracy of Q_{EC} -
determination

JYFLTRAP:

⁵⁰Mn and ⁵⁴Co Q_{EC} -values
checked and improved in the
last week.

Slight deviation in Q_{EC} -value.
Will slightly increase Ft -values

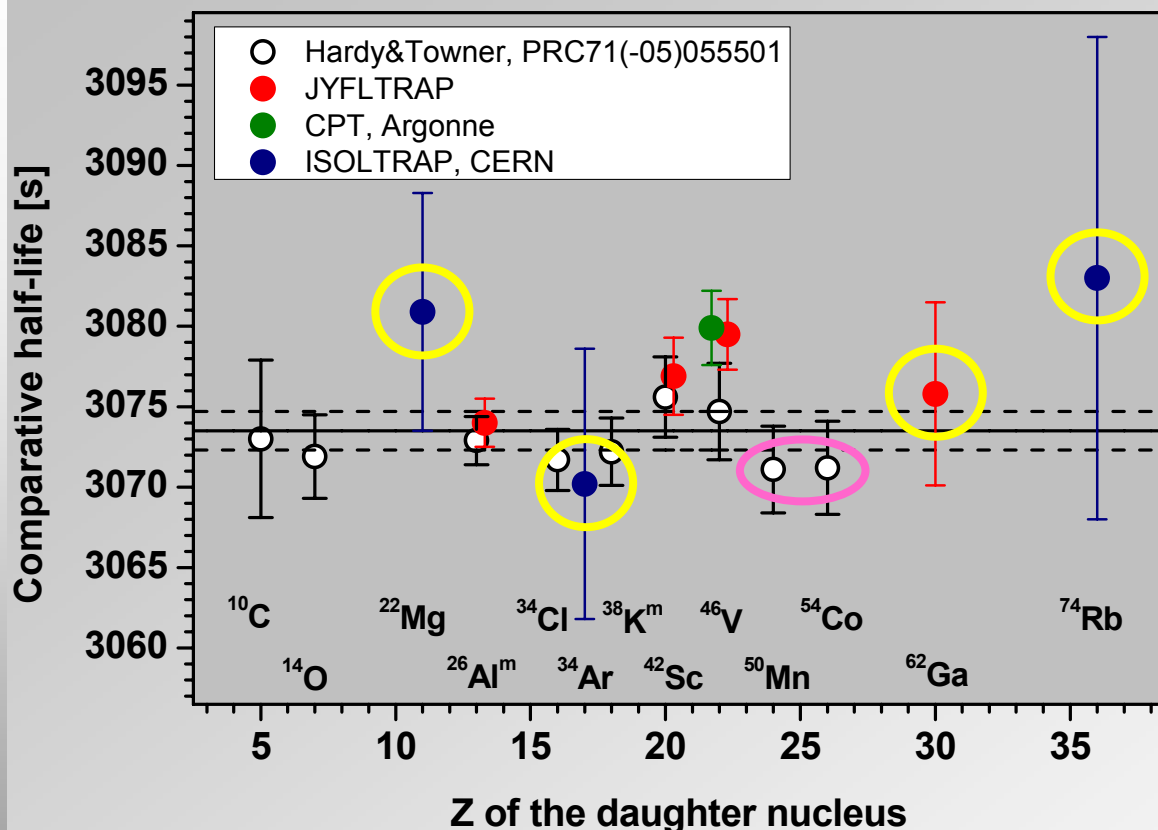
Q_{EC} -values of ²⁶Si and ⁴²Ti in
progress

Half-lives:

³⁴Ar and ³⁴Cl, Texas A&M
V.E. Iacob *et al.*, PRC 74
(2006) 055502

⁵⁰Mn, Auckland/Canberra
Barker & Byrne, PRC 73 (2006)
064306

Experimental status June-2007



^{22}Mg , ^{34}Ar , ^{62}Ga and ^{74}Rb :
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^{74}Rb	A. Kellerbauer <i>et al.</i> , Phys. Rev. Lett. 93 (2004) 072502

Implications on V_{ud} and the unitarity of CKM

Situation as now:

J. Hardy CKM2006 + priv. comm.

$$F_t = 3073.9(8)$$

$$V_{ud} = 0.97378(27)$$

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.9992(11)$$



Compare to 2005 survey
Hardy & Towner, PRC71 (2005) 055501

$$V_{ud} = 0.97380(40)$$

Improved precision mainly due to
improved radiative correction ΔR
Marciano & Sirlin, PRL96 (2006) 032001

$$< 0.0001$$

$$0.0509(9)$$



M. Moulson, CKM2006:
 V_{us} from $Kl3$ 0.2257 ± 0.0020

$$0.9483(5)$$



Nuclear $0+ \rightarrow 0+$	0.9738 ± 0.0003
Neutron decay	0.9745 ± 0.0018
Pion beta decay	0.9751 ± 0.0027

Acknowledgements:

IGISOL-crew:

V.-V. Elomaa
T. Eronen
U. Hager
J. Hakala
A. Jokinen
A. Kankainen
I. Moore
H. Penttilä
S. Rahaman
S. Rinta-Antila
J. Rissanen
T. Sonoda
C. Weber
J. Äystö



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V. Kolhinen and J. Szerypo, LMU, Munchen, Germany
J. Hardy, Texas A&M, USA

